

Testing the CGC with RHIC forward data

Javier L Albacete



Workshop on Forward Physics at RHIC, Jul-30-Aug 1st
Brookhaven National Lab

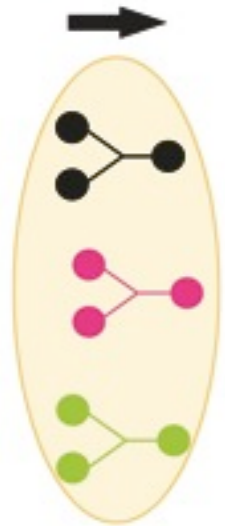
What the CGC is about : coherence effects in high energy QCD (small-x)

High gluon densities in the projectile/target

Saturation: gluon self-interactions tame the growth of gluon densities towards small-x

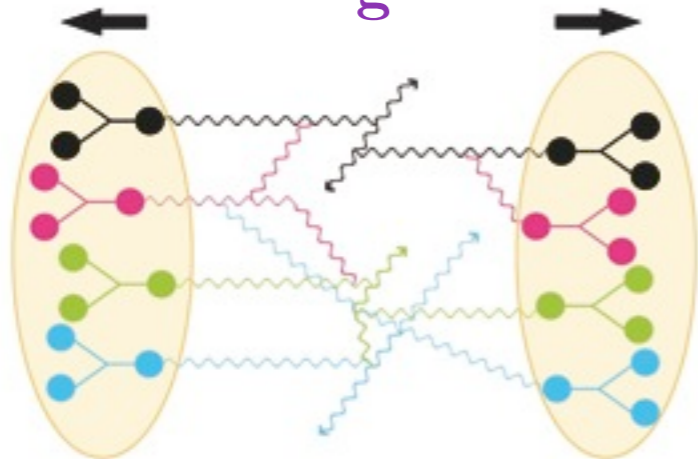
$$\frac{\partial \phi(\mathbf{x}, \mathbf{k}_t)}{\partial \ln(\mathbf{x}_0/\mathbf{x})} \approx \underbrace{\mathcal{K} \otimes \phi(\mathbf{x}, \mathbf{k}_t)}_{\text{radiation}} - \underbrace{\phi(\mathbf{x}, \mathbf{k}_t)^2}_{\text{recombination}}$$

$$\mathbf{k}_t \lesssim Q_s(\mathbf{x})$$



Breakdown of independent particle production

$$\mathcal{A}(\mathbf{k} \lesssim Q_s) \sim \frac{1}{g} \quad g\mathcal{A} \sim \mathcal{O}(1)$$



What the CGC is about : coherence effects

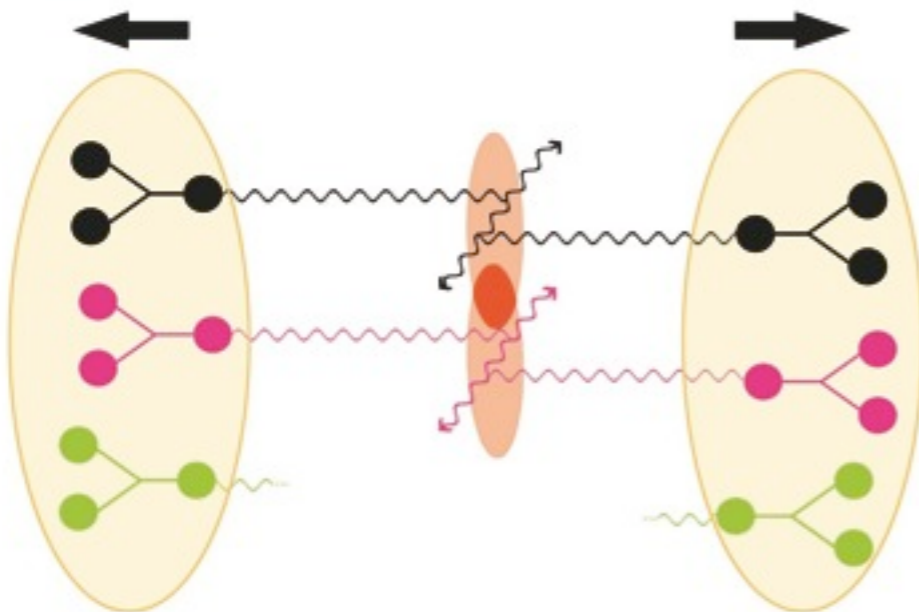
High gluon densities in the projectile/target

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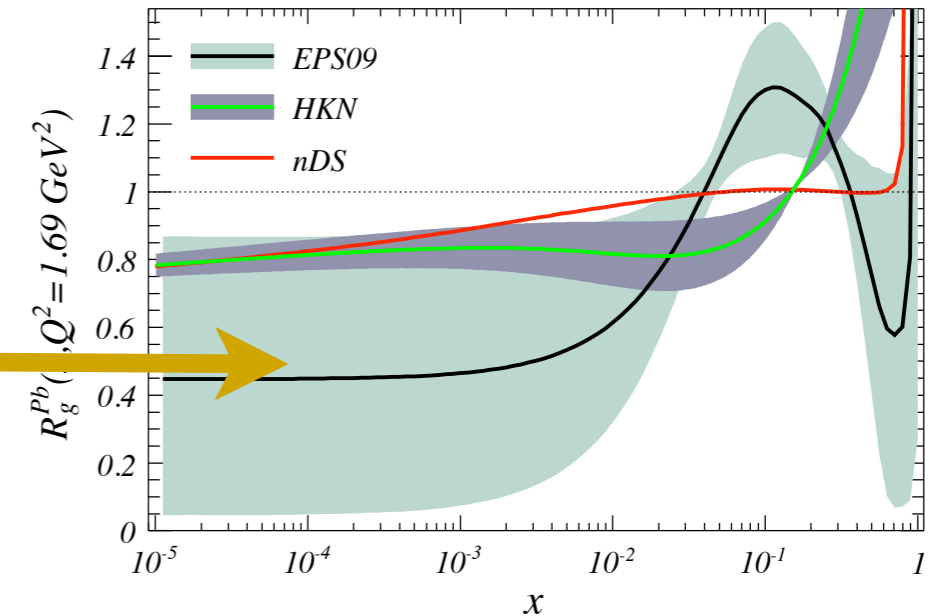
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Breakdown of independent particle production

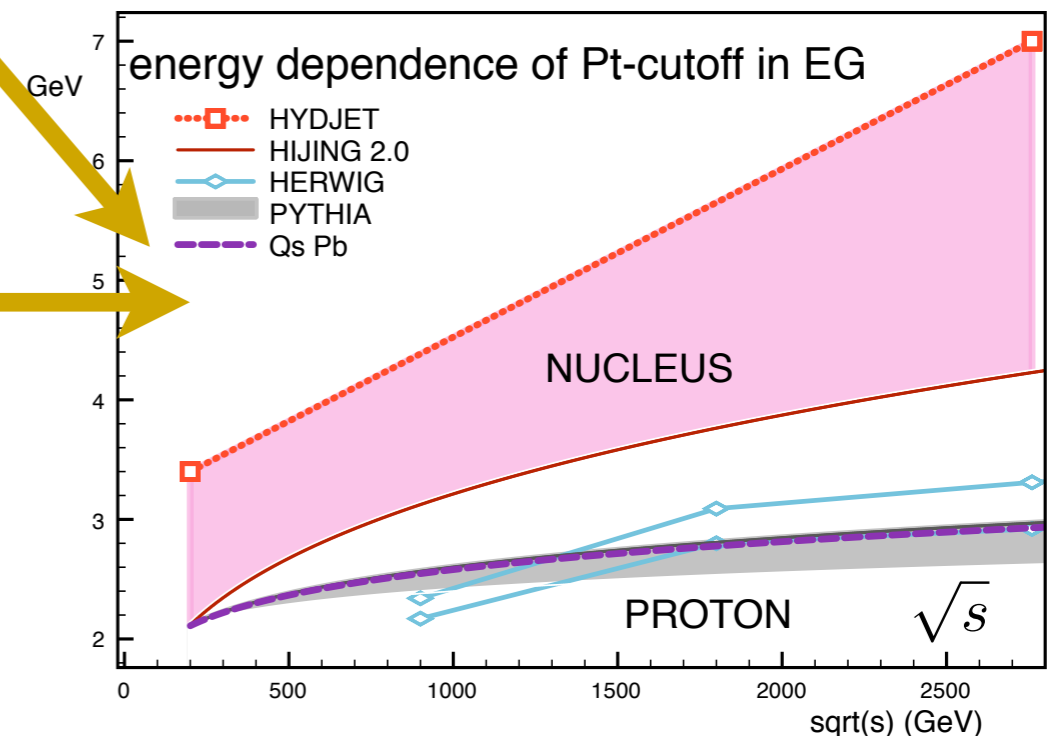


HIC phenomenology

- Nuclear shadowing, String fusion, percolation

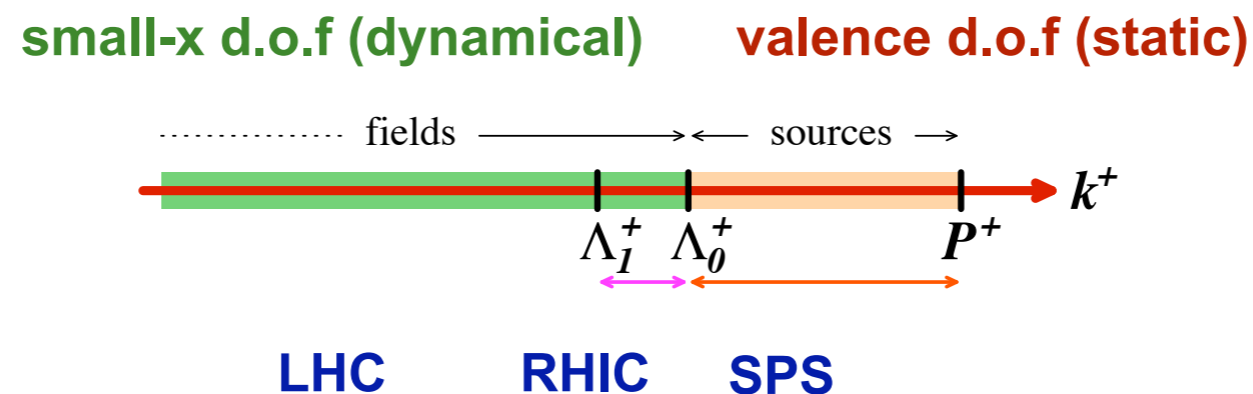


- Resummation of multiple scatterings
- kt-broadening
- Energy dependent cutoff in event generators



OUTLINE

- Coherence effects are essential for the description of data in HIC collisions (RHIC, LHC)
- The presence of a semi-hard dynamical scale --the saturation scale-- + non-linear dynamics led to semi-quantitative predictions later confirmed by data
 - $\sim N_{part}$ scaling and energy dependence of total multiplicities **Kharzeev-Levin-Nardi** **JLA-Armesto-**
 - Continuous depletion of nuclear modification factors with increasing hadron rapidity in dA collisions **Kovner-Salgado-**
 - Angular decorrelation of hadron pairs produced at forward rapidities in dA collisions, **Marquet** **Wiedeman**
- Getting quantitative: Is the CGC effective theory (at its present degree of accuracy) the best suited framework to quantify coherence phenomena in HI collisions at RHIC and the LHC?
 - Control of missing dynamical effects: are RHIC and LHC energies large enough for the applicability of the CGC?
 - Control of higher order terms in the perturbative series
 - Do we have enough empiric info (i.e. data) to constrain the NP parameters of the theory?



Color Glass Condensate phenomenology tools (in half a slide)

1.- (classical) Ab initio calculation of nuclear structure functions (small-x gluon distributions)

McLerran-Venugopalan model ($x_0 \sim 0.01$). Valid for large nucleus $gA^{1/3} \gg 1$

2.- (quantum) Nonlinear renormalization group equations towards small-x

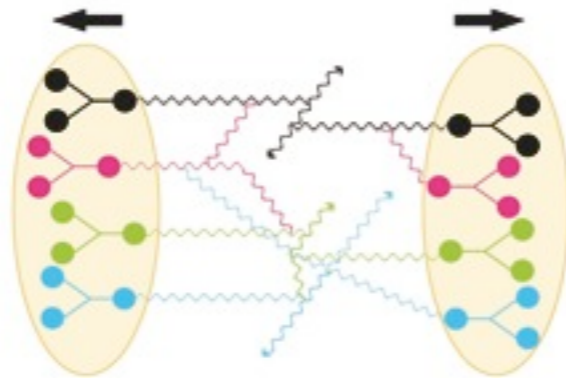
BK-JIMWLK eqns ($x < x_0 \sim 0.01$)

$$\frac{\partial \phi(x, k)}{\partial \ln(1/x)} = \mathcal{K} \otimes \phi(x, k) - \phi^2(x, k) \quad \frac{\partial W[\rho]}{\partial Y} = \dots$$

3.- Production processes

$$\frac{dN^{AB \rightarrow X}}{d^3p_1 \dots} [\phi(x, k); W_Y[\rho]]$$

CYM,
kt-factorization
hybrid formalism...



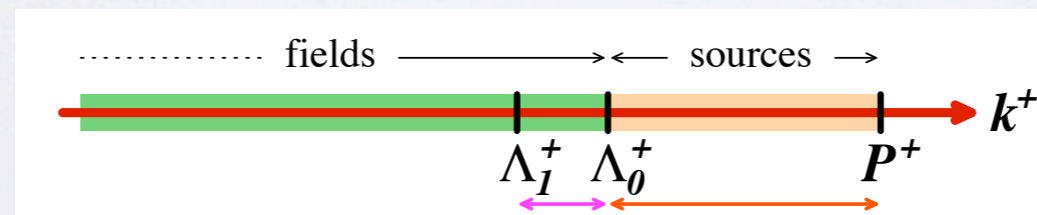
$$\mathcal{A}(k \lesssim Q_s) \sim \frac{1}{g}$$

$$g\mathcal{A} \sim \mathcal{O}(1)$$

The eikonal (recoil-less) approximation is central in the CGC:

small-x d.o.f (dynamical)

valence d.o.f (static)



LHC

RHIC

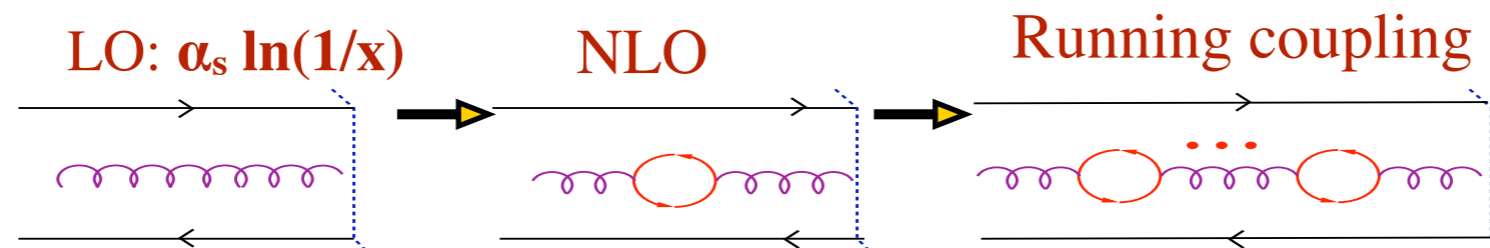
SPS

(brief and incomplete) CGC Theory Status: Entering the NLO era

Evolution Equations: $\frac{\partial \phi(x, k)}{\partial \ln(1/x)} = \mathcal{K} \otimes \phi(x, k) - \phi^2(x, k) \quad \frac{\partial W[\rho]}{\partial Y} = \dots$

- ✓ - Running coupling kernel in BK evolution for the 2-point function Kovchegov Weigert Gardi Balitsky
- ✗ - Full NLO kernel for BK-JIMWLK [Balitsky Chirilli]
- ✗ - Analytic [Triantafyllopoulos] and numerical [T. Lappi et.al] solutions of full B-JIMWLK hierarchy for n-point functions

- ...



Production processes $\frac{dN^{AB \rightarrow X}}{d^3p_1 \dots} [\phi(x, k); W_Y[\rho]]$

- ✗ - Running coupling and full NLO corrections to kt-factorization [Kovchegov, Horowitz, Balitsky, Chirilli]
- ✓ - Inelastic terms in the hybrid formalism [Kovner-Altinoluk]
- ✓ - Hadron-hadron, hadron-photon* correlations
- ✗ - Factorization of multiparticle production processes at NLO
- ✗ - DIS NLO photon impact factors [Chirilli]
- ...

Used in phenomenological works? ✓ Yes ✗ No ✓ A bit :)

Data??

Empiric information needed to constrain:

- **Non-perturbative parameters:** initial conditions for BK-JIMWLK evolution, impact parameter
- **K-factors** to account for higher order corrections (effectively also for missing high- x , Q^2 contributions, energy-conservation corrections etc)

:)

proton

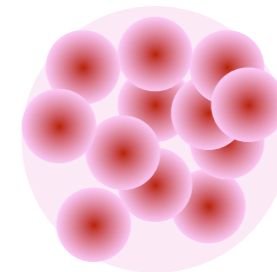
- **Abundant high quality data at small- x**
- Good simultaneous description of e+p and p+p data
- Global rcBK fits to constrain gluon distribution



:|

nucleus

- **Fewer data at small- x**
- LHC Pb+Pb data (difficult...)
- EIC and pPb @ LHC data to come...
- RHIC dAu forward data provides the best testing ground of the CGC

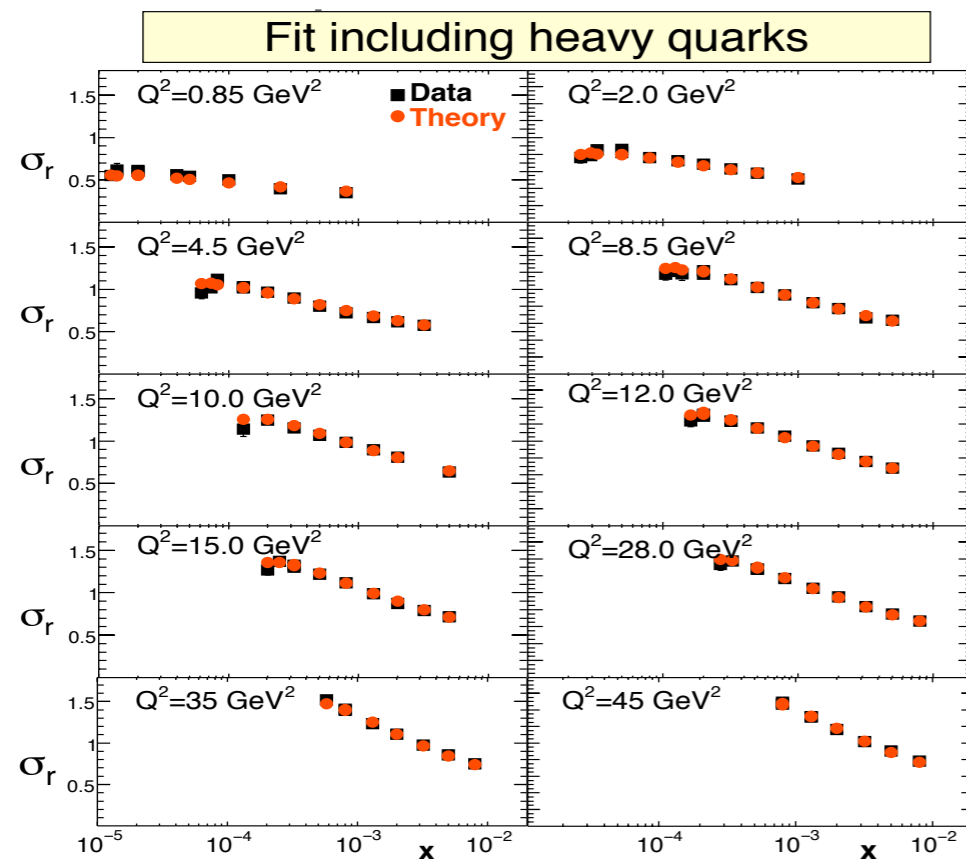


modelling!



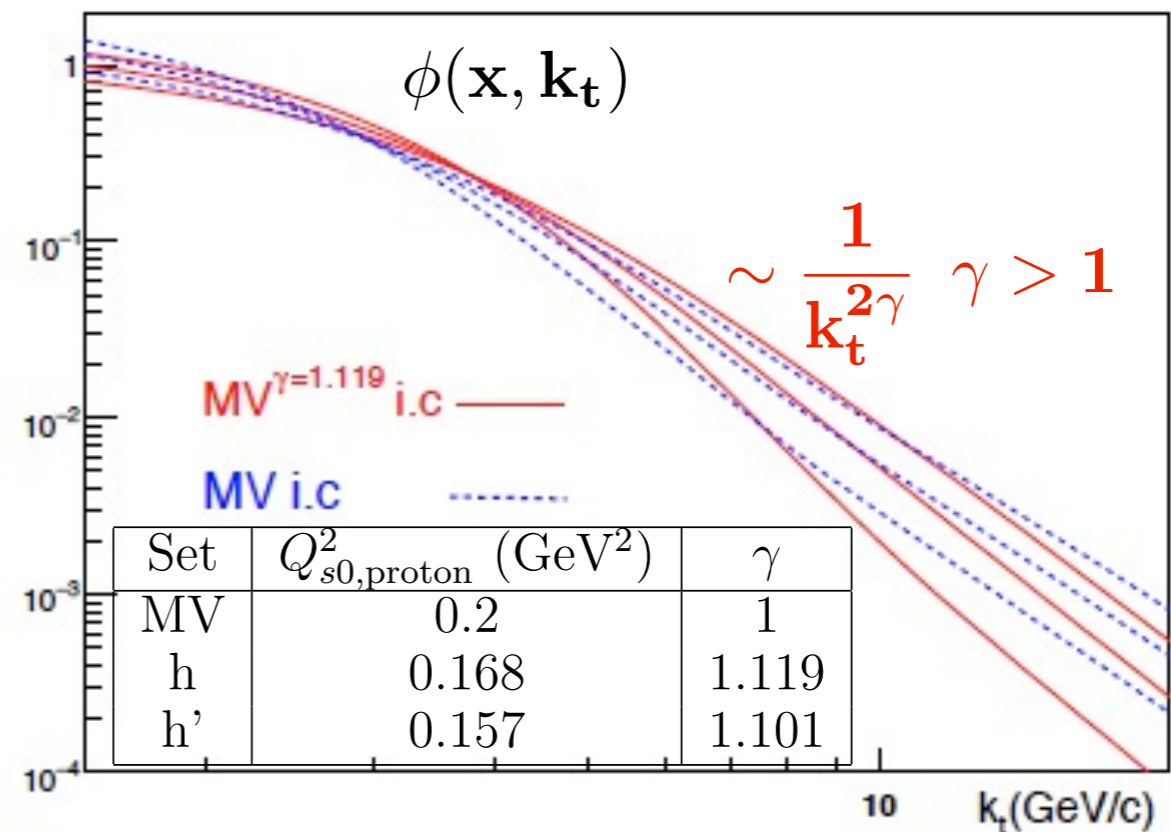
The baseline: proton collisions

1. Global fits to e+p data at small-x



JLA-Armesto-Milhano-Quiroga-Salgado

2. Extract NP fit parameters



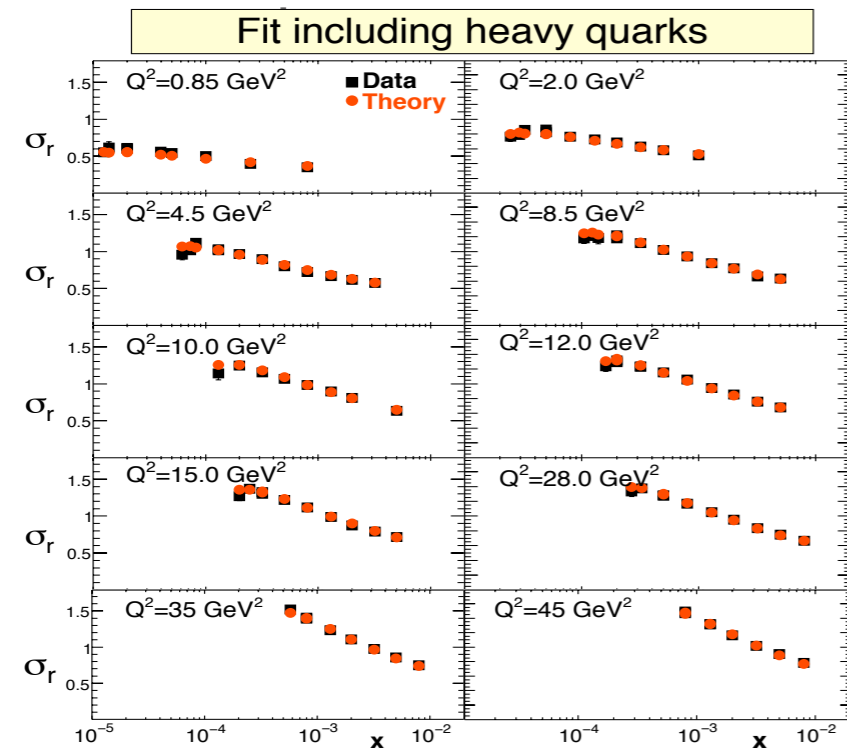
$$\mathcal{N}^{MV}(r, x_0 = 10^{-2}) = 1 - \exp \left[- \left(\frac{r^2 Q_{s0}^2}{4} \right)^\gamma \ln \left(\frac{1}{r \Lambda_{QCD}} \right) \right]$$

- Fits to e+p data clearly prefer $\gamma > 1$.
- MV ($\gamma = 1$) model seems not to work well for protons...
- Possible explanation: subleading in density corrections to the MV model yield $\gamma > 1$ [Dumitru & Pereska 11](#)

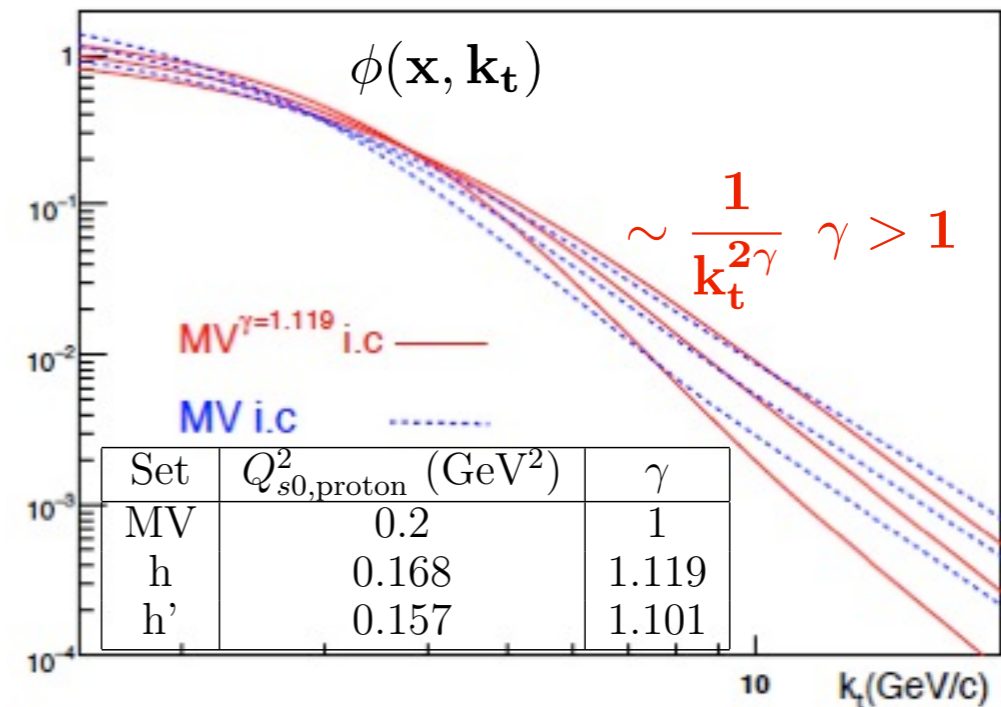
The baseline: proton collisions

Talk by P. Quiroga

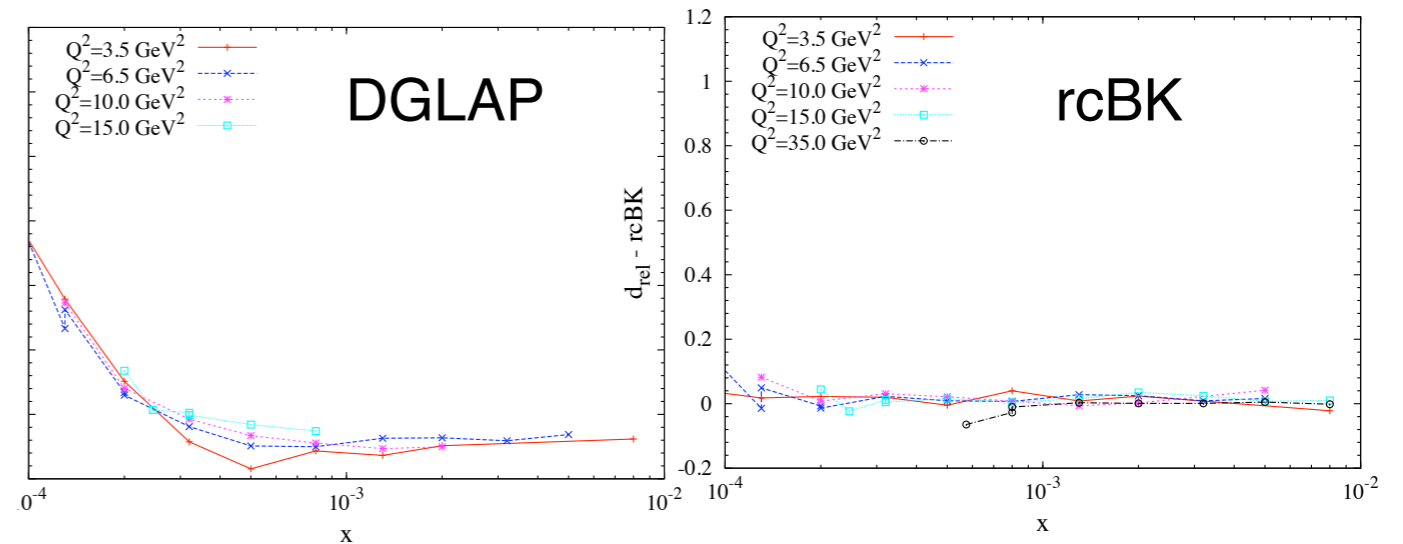
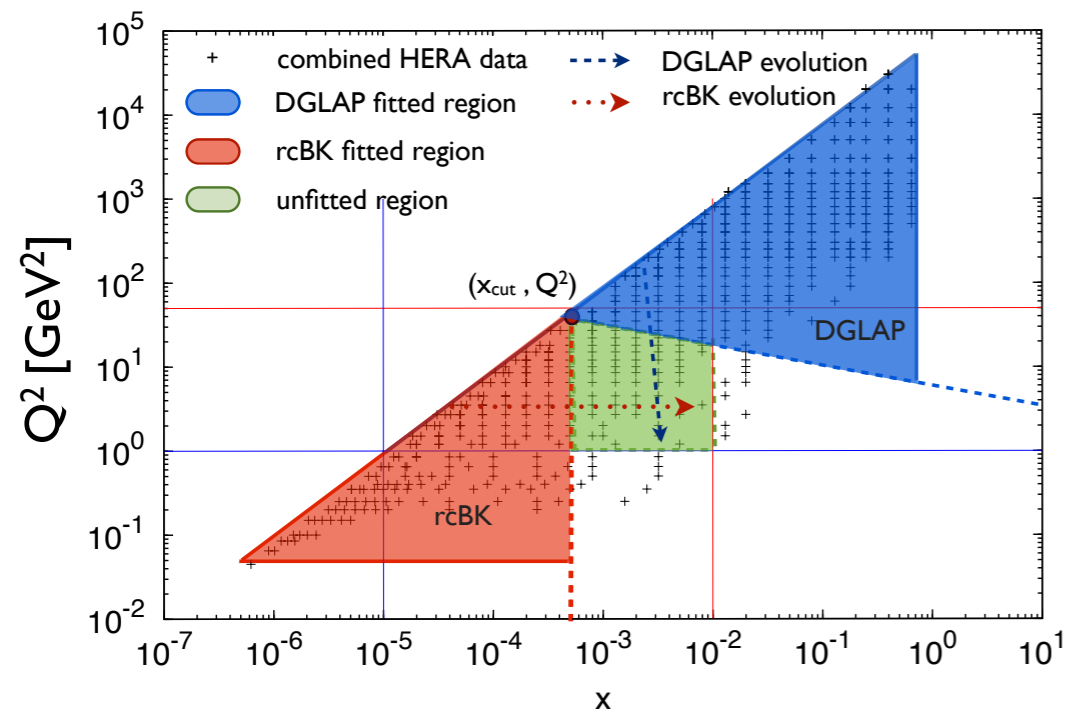
1. Global fits to e+p data at small-x



2. Extract NP fit parameters



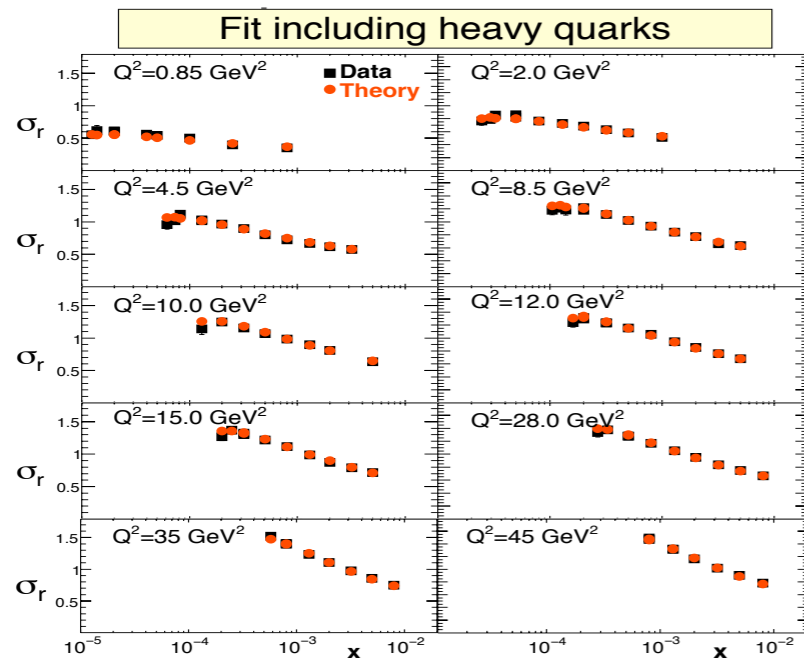
3. Run consistency and stability checks



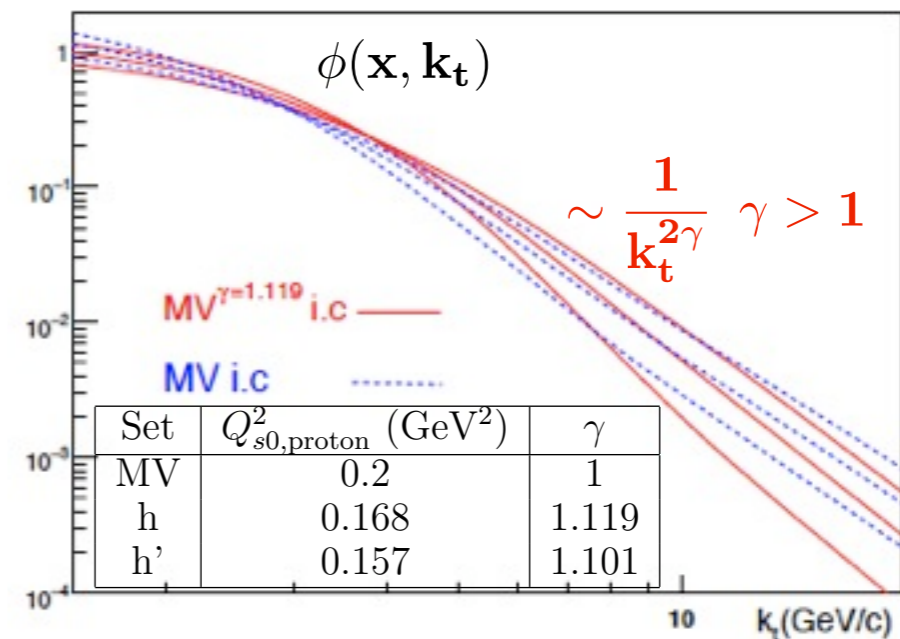
rcBK fits more stable than DGLAP fits at small-x!!!

The baseline: proton collisions

1. Global fits to e+p data at small-x

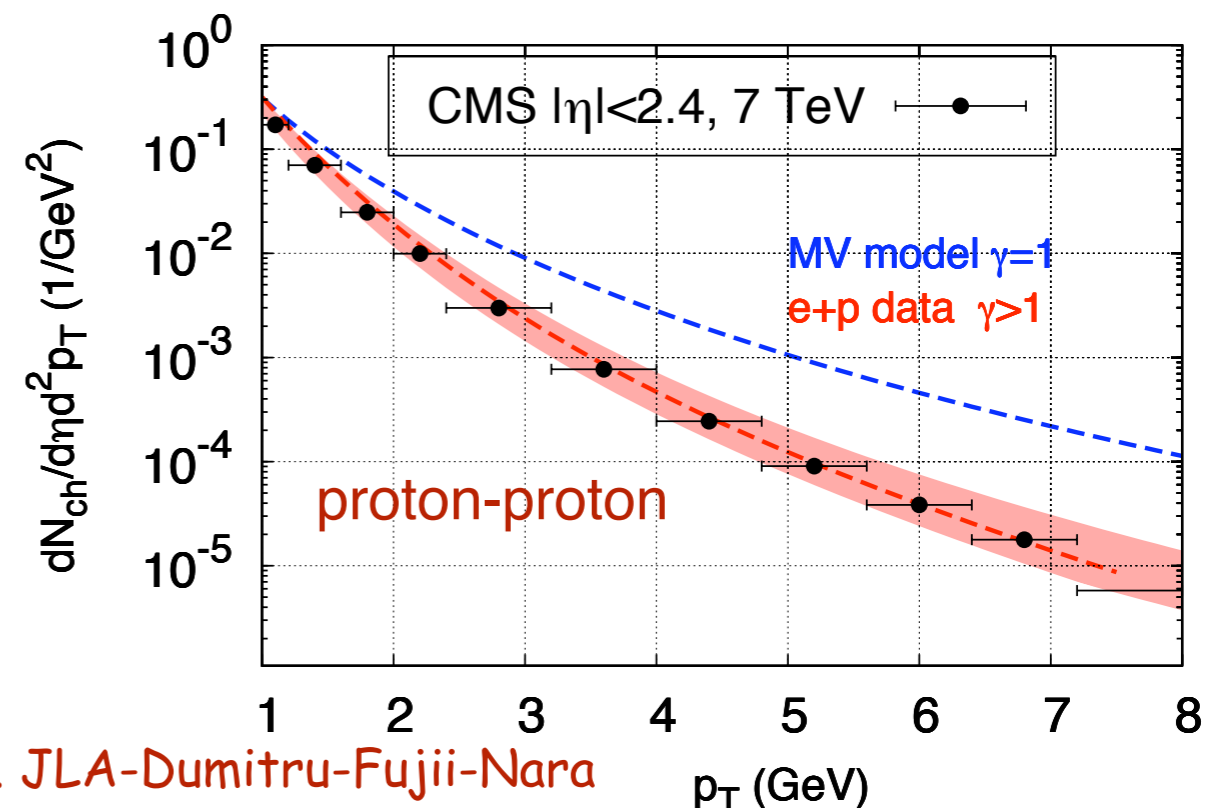
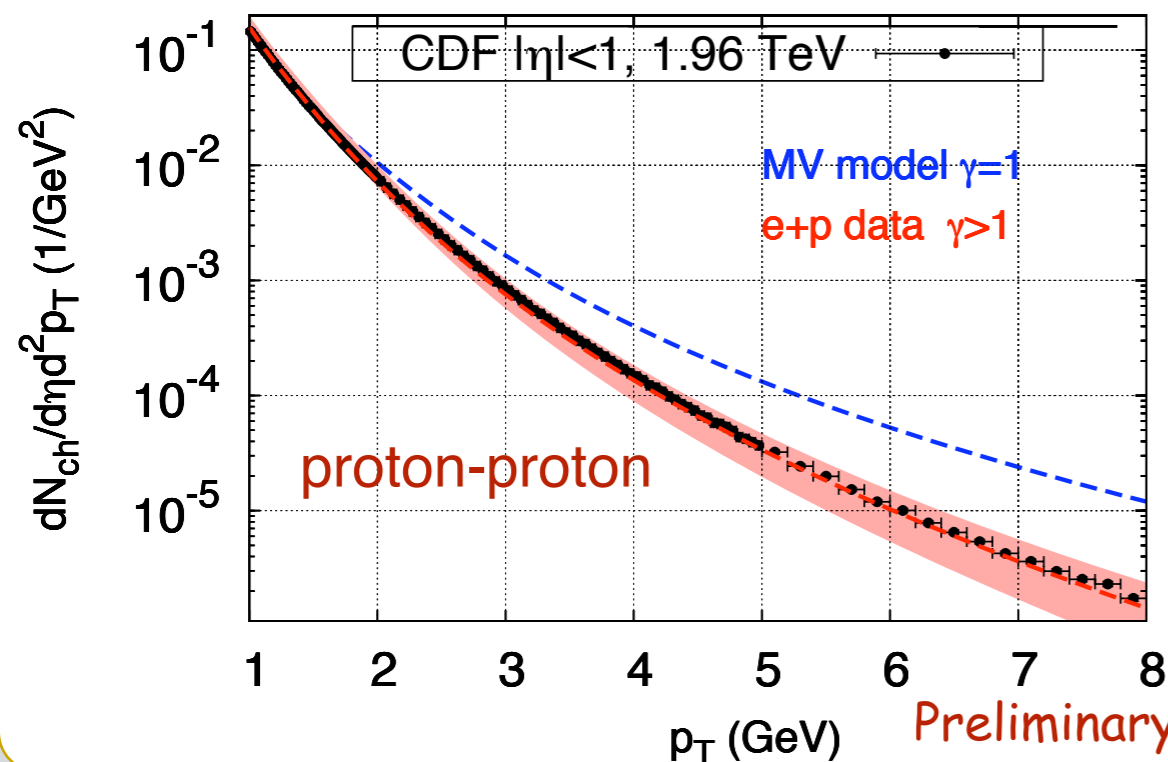


2. Extract NP fit parameters



4. Apply gained knowledge in the study of other systems (theory driven extrapolation)

LO kt-factorization: $\frac{dN^g}{d\eta d^2p_t} \sim K \alpha_s(Q_r^2) \phi(x_1, k_t) \otimes \phi(x_2, k_t - p_t) \otimes FF(Q_f^2)$



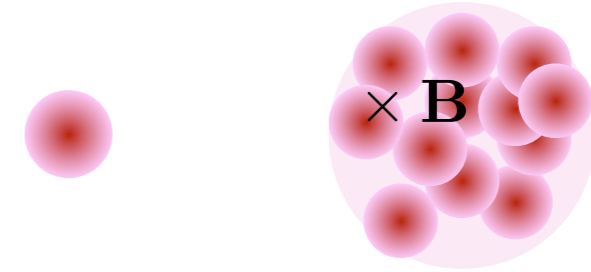
Nuclear ugd's and nuclear modification factors

1. Setting up the evolution

$$\phi^{\text{Pb}}(\mathbf{x}_0, \mathbf{k}_t, \mathbf{B}) = \phi^{\text{P}}(\mathbf{x}_0, \mathbf{k}_t; \{Q_{s0,p}^2 \rightarrow Q_{s0,\text{Pb}}^2(\mathbf{B}); \gamma\})$$

$$\downarrow$$

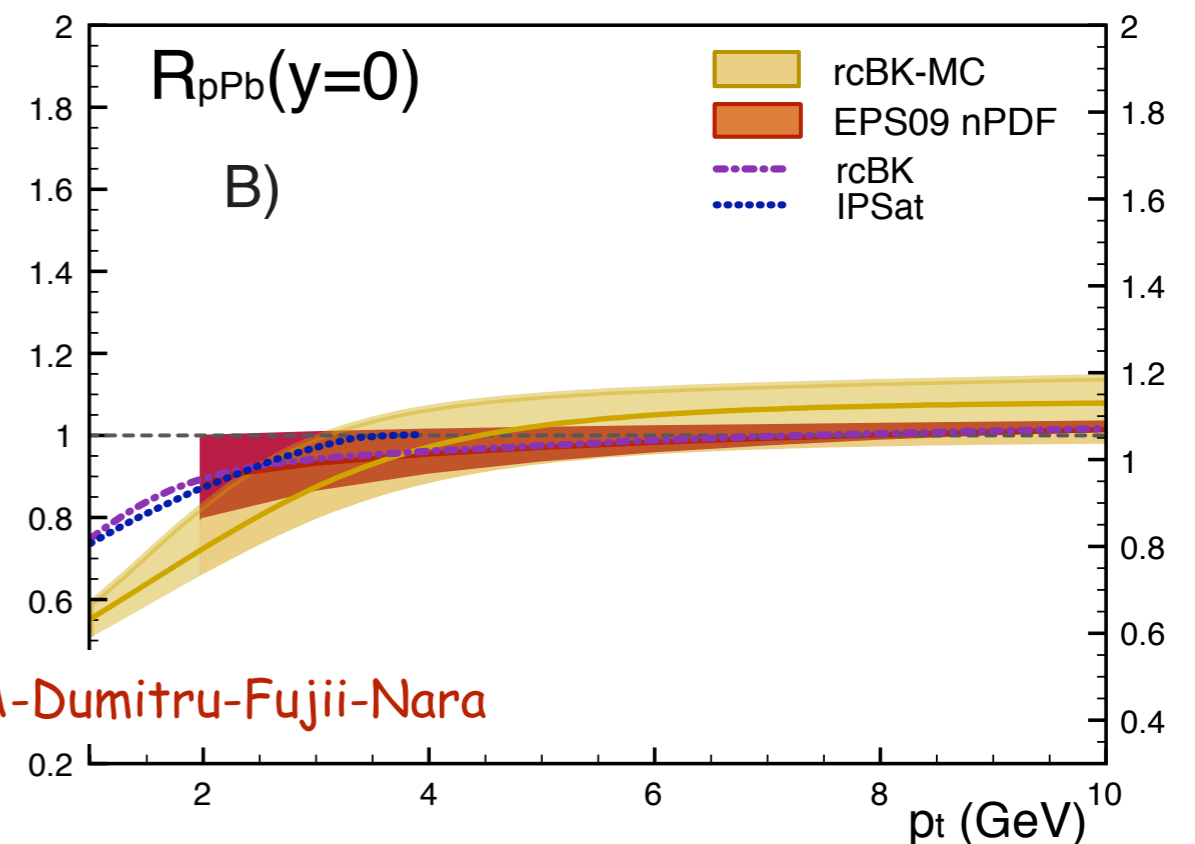
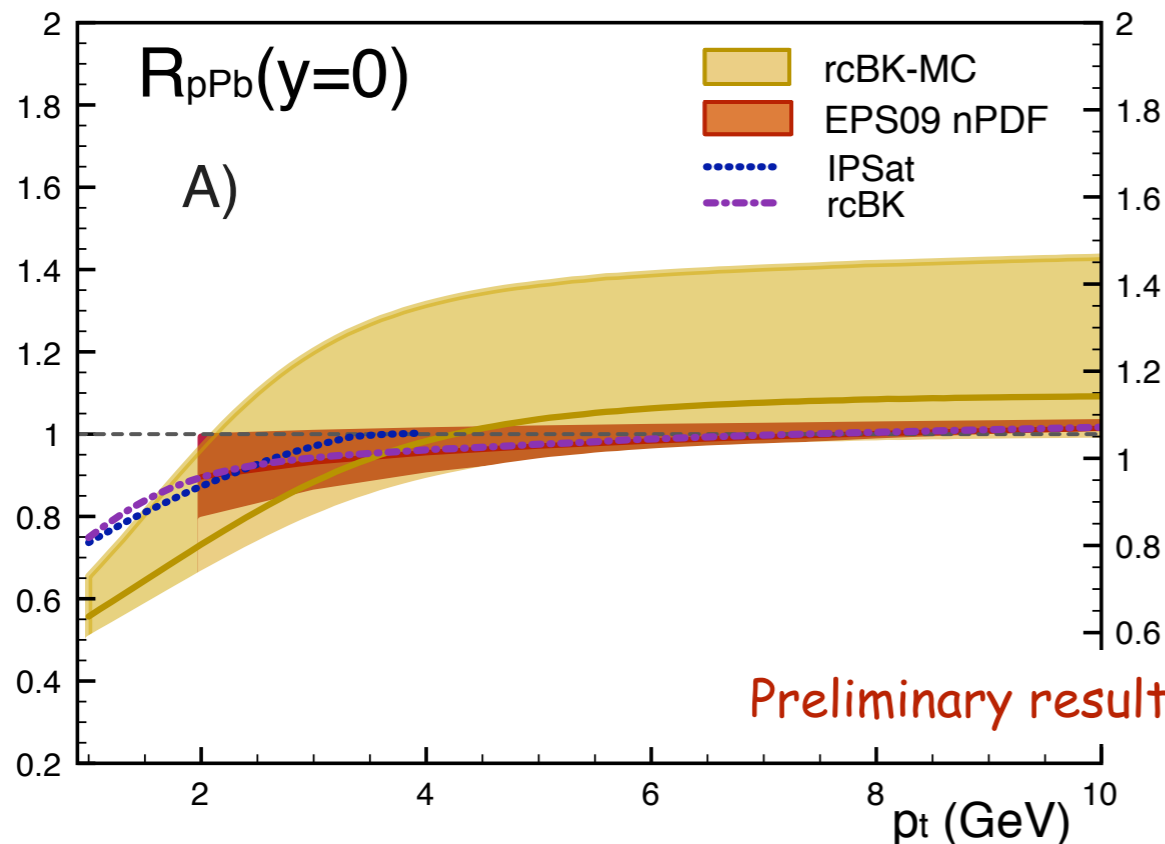
$$\phi^{\text{Pb}}(\mathbf{x}, \mathbf{k}_t, \mathbf{B}) = \text{rcBK}[\phi^{\text{Pb}}(\mathbf{x}_0, \mathbf{k}_t, \mathbf{B})]$$



A) Most “natural” option: $Q_{s0,\text{Pb}}^2(\mathbf{B}) = \mathbf{T}_A(\mathbf{B}) Q_{s0,p}^2$ $\gamma^{\text{Pb}} = \gamma^{\text{P}} (> 1)$

PROBLEM: yields $R_{\text{pPb}} > 1$ at high transverse momentum

B) Possible solution $Q_{s0,\text{Pb}}^2(\mathbf{B}) = \mathbf{T}_A(\mathbf{B})^{1/\gamma} Q_{s0,p}^2$ and/or $\gamma^{\text{Pb}} = 1(\text{MV}) + \frac{\#}{A^2/3}$

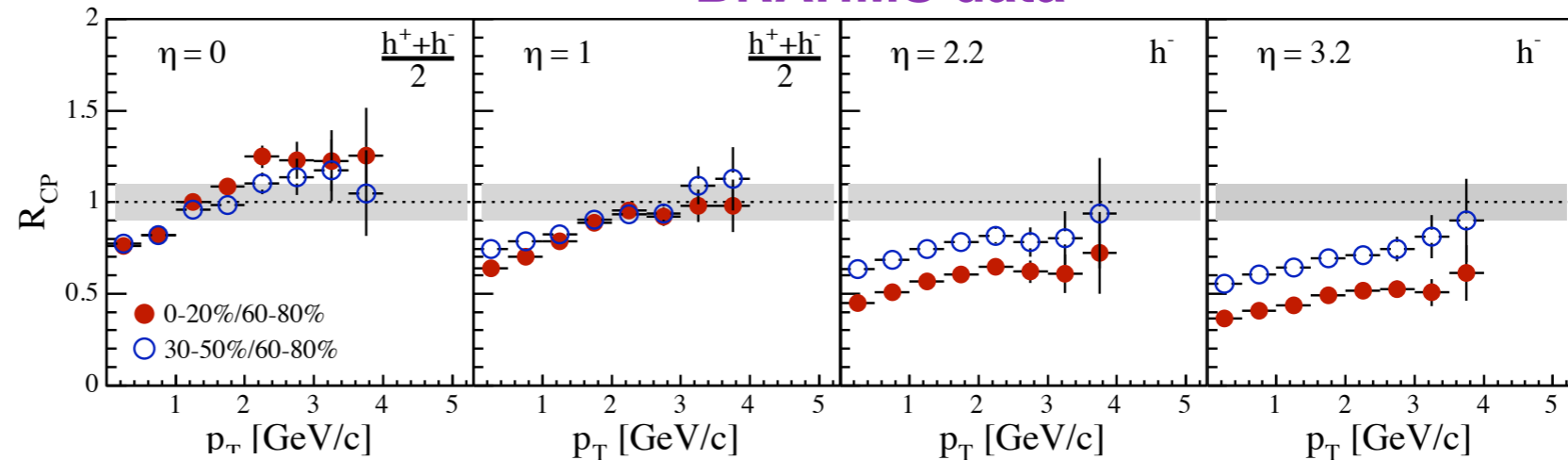


Preliminary results. JLA-Dumitru-Fujii-Nara

Single inclusive forward particle production in p(d)-A collisions

$$R_{pA} = \frac{\frac{dN_{pA}}{dy d^2 p d^2 b}}{A^{1/3} \frac{dN_{pp}}{dy d^2 p d^2 b}}$$

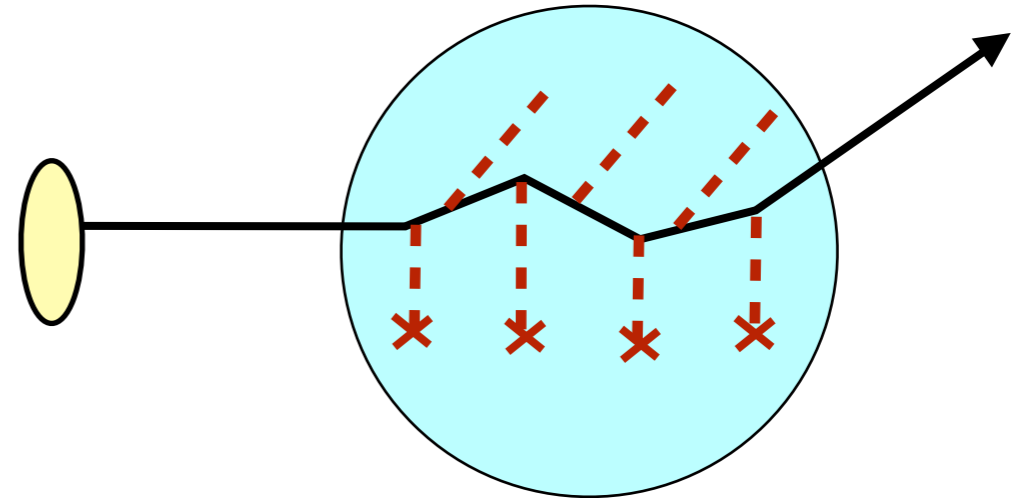
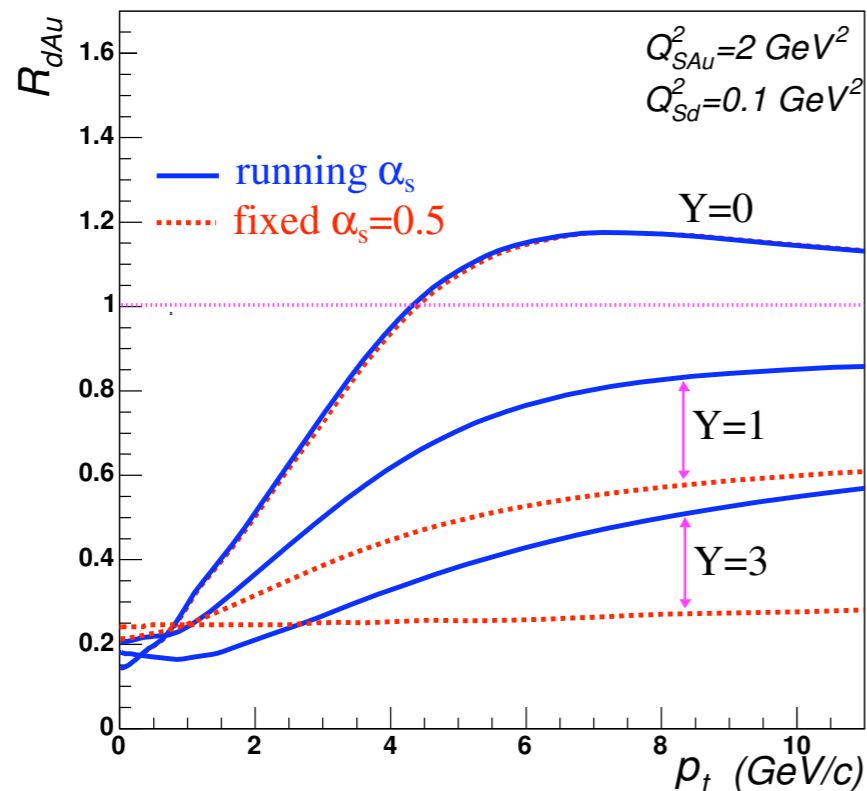
BRAHMS data



- **CGC**: Forward suppression originates in the dynamical shadowing generated by the **quantum non-linear BK-JIMWLK** evolution towards small- x

- Alternative: **Energy loss** arising from induced gluon bremsstrahlung (stronger in nucleus than in proton)

Non-Linear Evolution of Cronin Enhancement



Probability of not losing energy:

$$P(\Delta y) \approx e^{-n_G(\Delta y)} \approx (1 - x_F)^{\#}$$

Kopeliovich et al, Frankfurt Strikman

Single inclusive forward particle production in p(d)-A collisions

Hybrid formalism (Dumitru-Jalilian-Marian):

$$x_{1(2)} \sim \frac{m_t}{\sqrt{s}} \exp(\pm y_h)$$

large-x parton from proj. (pdf)

$(p_t, y_h \gg 0)$

small-x glue from target (CGC)

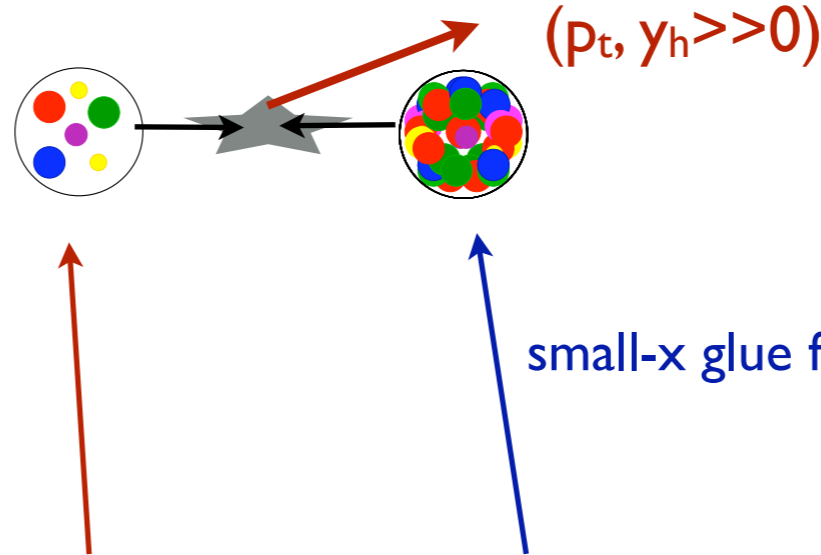
$$\frac{dN_h}{dy_h d^2p_t} = \frac{K}{(2\pi)^2} \sum_q \int_{x_F}^1 \frac{dz}{z^2} \left[x_1 f_{q/p}(x_1, p_t^2) \tilde{N}_F \left(x_2, \frac{p_t}{z} \right) D_{h/q}(z, p_t^2) \right. \\ \left. + x_1 f_{g/p}(x_1, p_t^2) \tilde{N}_A \left(x_2, \frac{p_t}{z} \right) D_{h/g}(z, p_t^2) \right] \longrightarrow \text{fragmentation}$$

Single inclusive forward particle production in p(d)-A collisions

Hybrid formalism (Dumitru-Jalilian-Marian):

$$x_{1(2)} \sim \frac{m_t}{\sqrt{s}} \exp(\pm y_h)$$

large-x parton from proj. (pdf)



small-x glue from target (CGC)

"elastic" term:

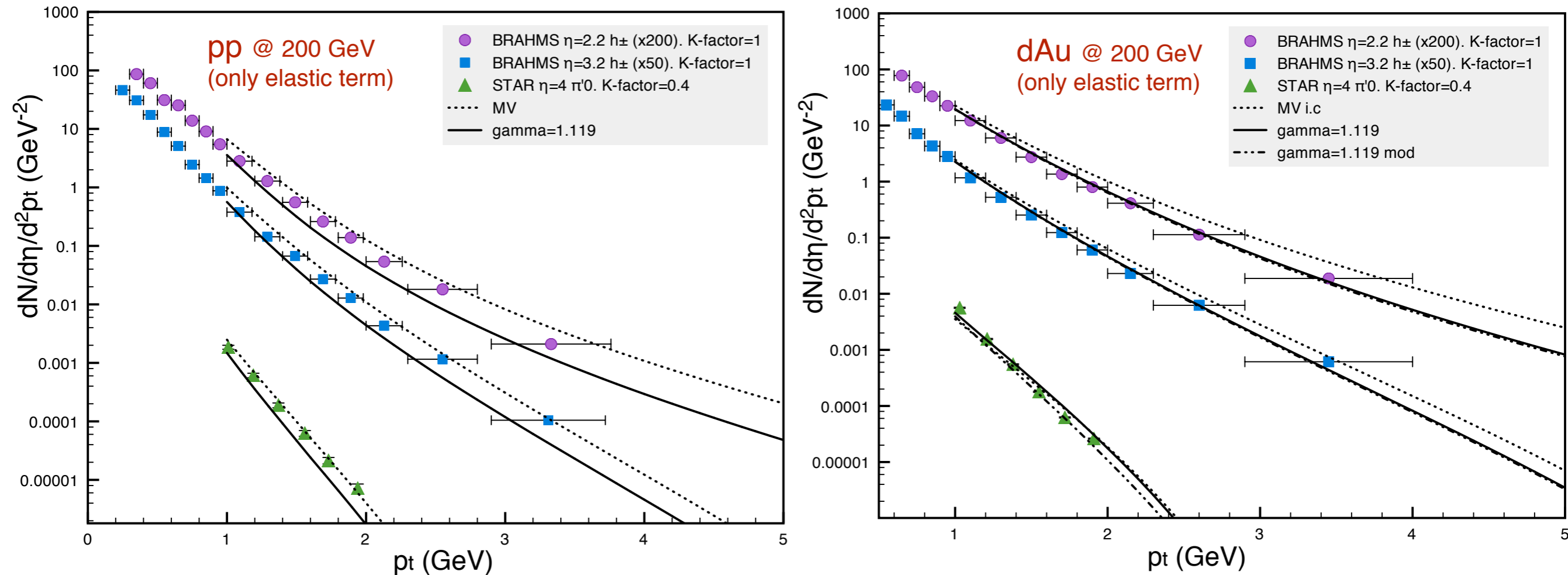
$$\frac{dN_h}{dy_h d^2p_t} = \frac{K}{(2\pi)^2} \sum_q \int_{x_F}^1 \frac{dz}{z^2} \left[x_1 f_{q/p}(x_1, p_t^2) \tilde{N}_F \left(x_2, \frac{p_t}{z} \right) D_{h/q}(z, p_t^2) \rightarrow \text{fragmentation} \right. \\ \left. + x_1 f_{g/p}(x_1, p_t^2) \tilde{N}_A \left(x_2, \frac{p_t}{z} \right) D_{h/g}(z, p_t^2) \right]$$

+ "inelastic" term (Altinoluk-Kovner): (Part of the NLO corrections)

$$+ \frac{\alpha_s(Q)}{2\pi^2} \int_{x_F}^1 \frac{dz}{z^2} \frac{z^4}{k^4} \int^Q \frac{d^2q}{(2\pi)^2} q^2 \tilde{N}_F(x_2, q) x_1 \int_{x_1}^1 \frac{d\xi}{\xi} \sum_{i,j=q,\bar{q},g} w_{i/j}(\xi) P_{i/j}(\xi) f_j\left(\frac{x_1}{\xi}, Q^2\right) D_{h/j}(z, Q^2)$$

Single inclusive forward particle production in p(d)-A collisions

Good description of pp and dAu RHIC forward data using only the “elastic” LO term



JLA-Marquet '10; JLA-Dumitru-Fujii-Nara (preliminary)

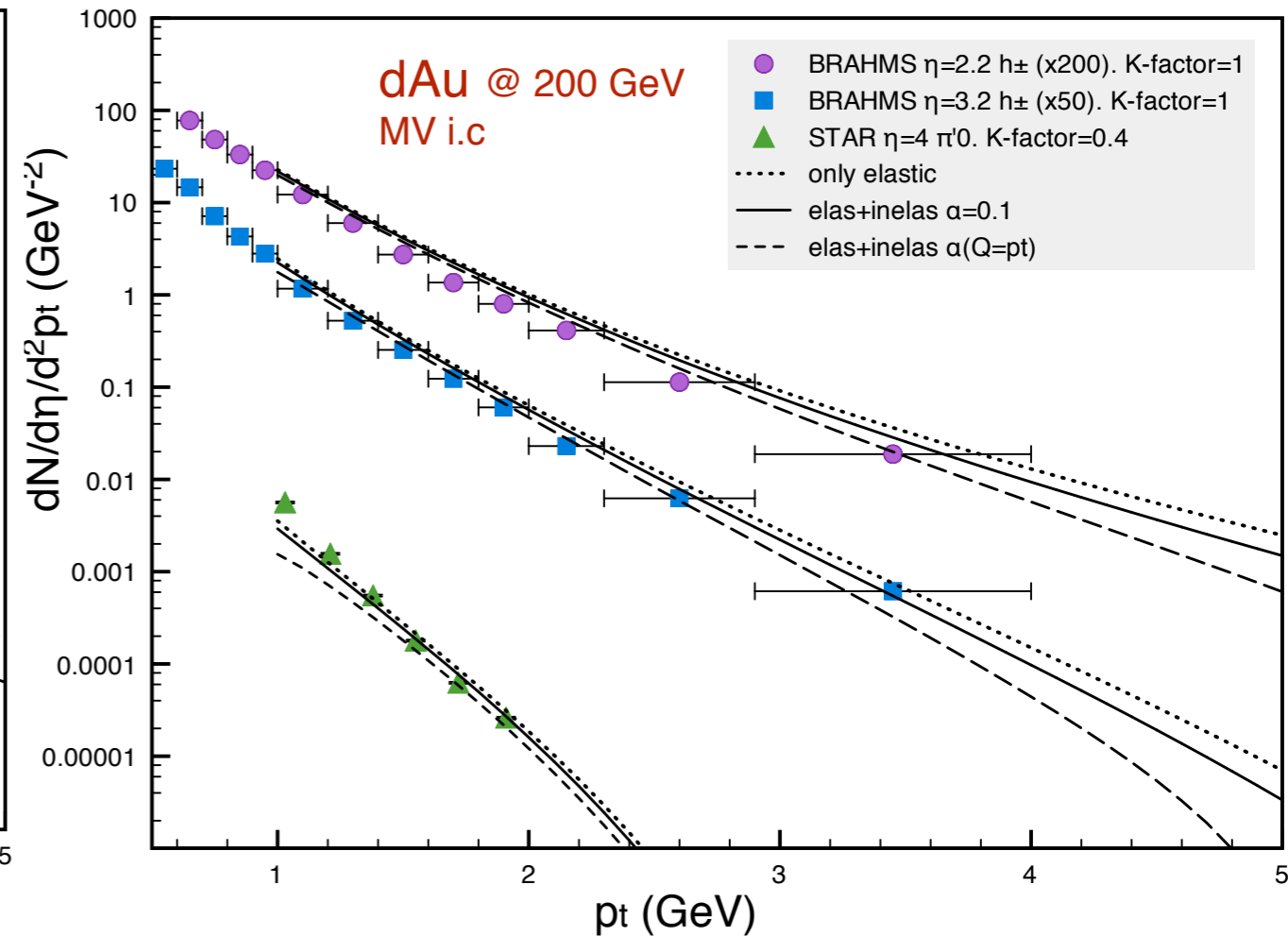
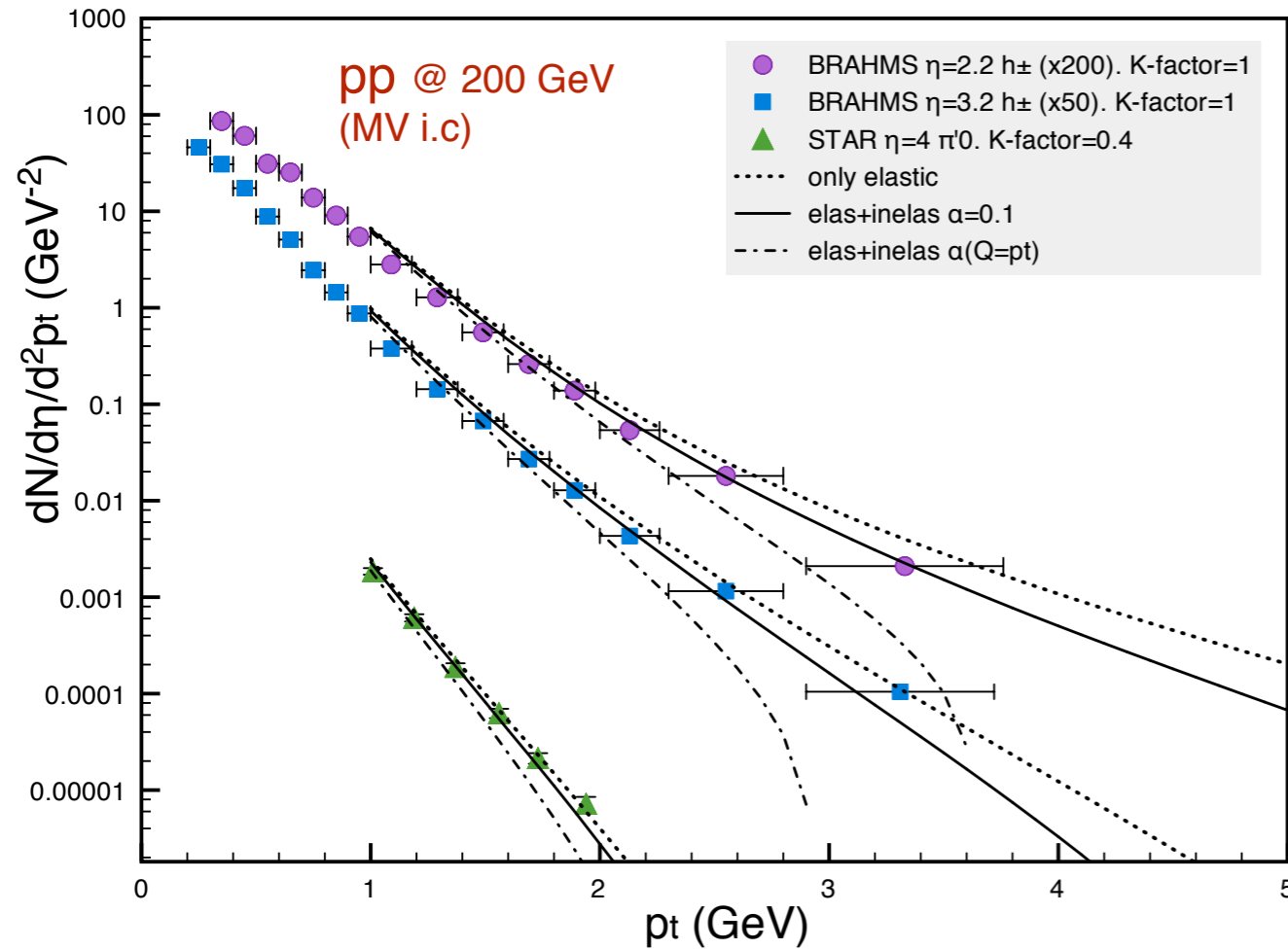
- However, RHIC data do not allow to determine the best i.c. for the nuclear UGD
- K-factor ~ 0.4 needed to describe the most forward pion data

Single inclusive forward particle production in p(d)-A collisions

NLO corrections brought by the “inelastic piece” may be large (preliminary results!!)

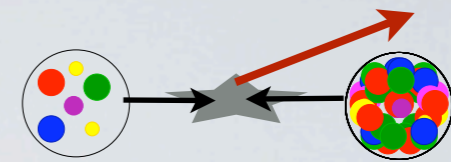
JLA-Dumitru-Fujii-Nara (preliminary)

Jalilian-Marian Rezaeian '11



- The inelastic term is negative for all values (y, p_t) explored in our work.
- Its relative magnitude wrt the elastic term decreases at small p_t or forward rapidities
- Changes in the scale for the running coupling affect significantly its absolute value (NNLO corrections needed?)

LHC: Moving forward: kt-factorization or hybrid?



$(p_t, y_h \gg 0)$

Yet another issue: Where to switch from kt-factorization to hybrid formalism? $x_{1(2)} \sim \frac{m_t}{\sqrt{s}} \exp(\pm y_h)$

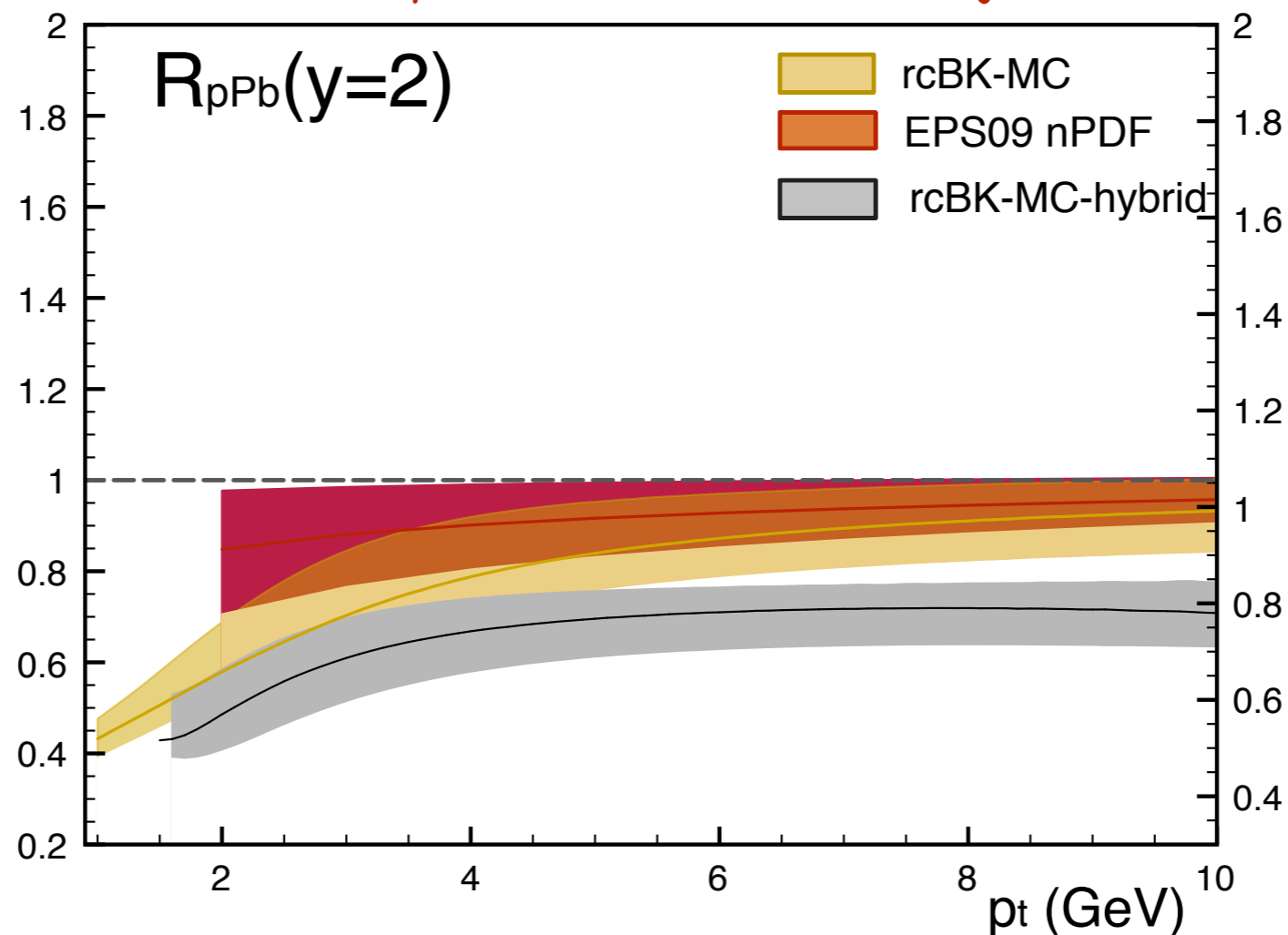
Midrapidity: kt-factorization:

$$\frac{dN^g}{d\eta d^2p_t} \sim \phi^P(\mathbf{x}_1) \otimes \phi^{Pb}(\mathbf{x}_2)$$

Forward rapidity: hybrid formalism

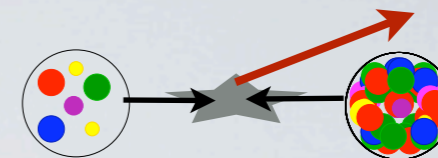
$$\frac{dN}{d\eta d^2p_t} \sim \text{pdf}^P(\mathbf{x}_1) \otimes \phi^{Pb}(\mathbf{x}_2)$$

Preliminary results. JLA-Dumitru-Fujii-Nara

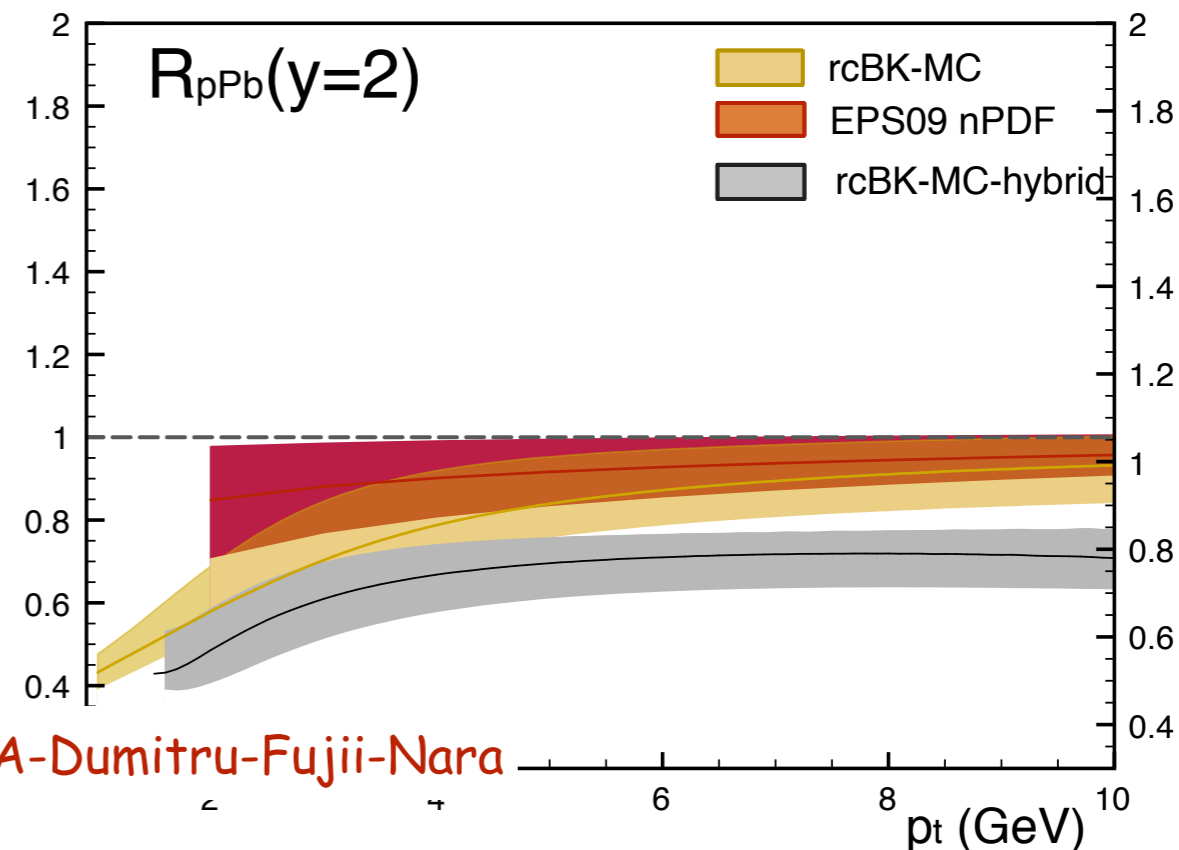
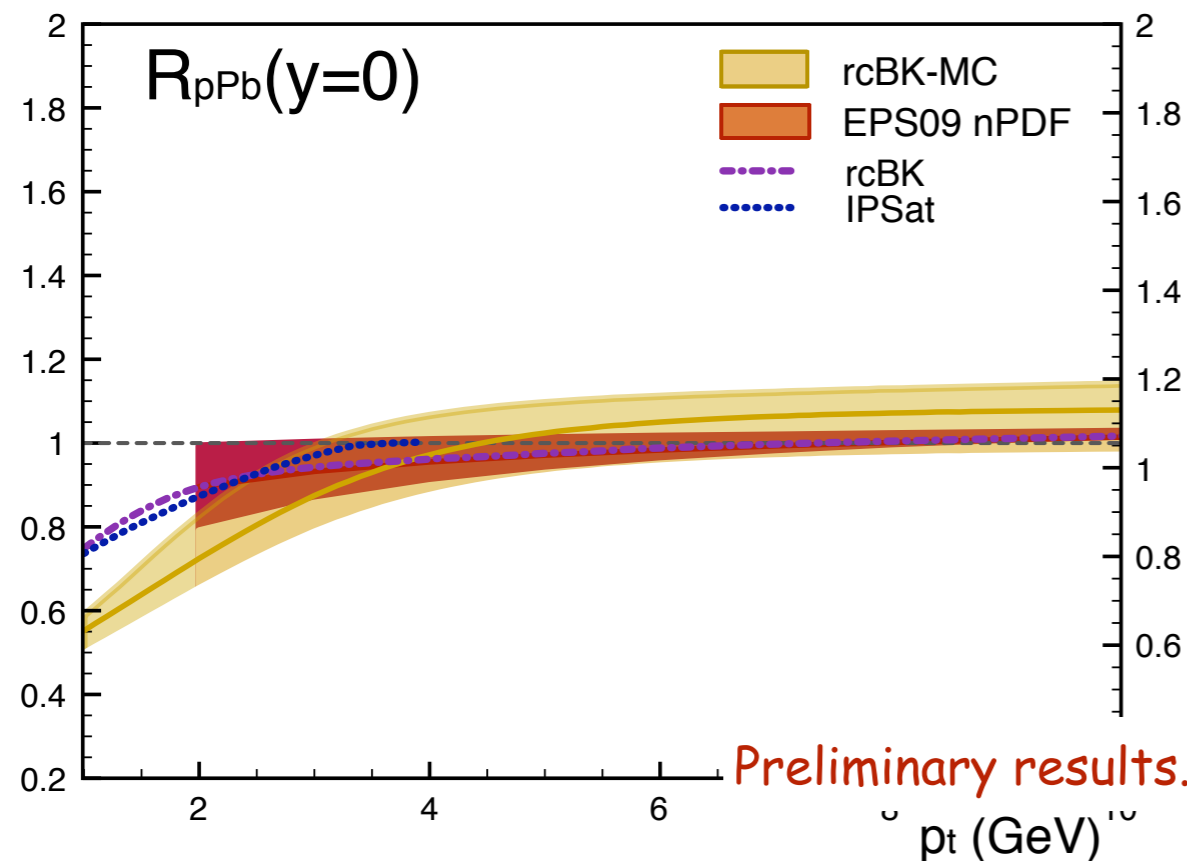


The inclusion of the inelastic term brings closer the hybrid and kt-fact results **Jalilian-Marian & Rezaeian**

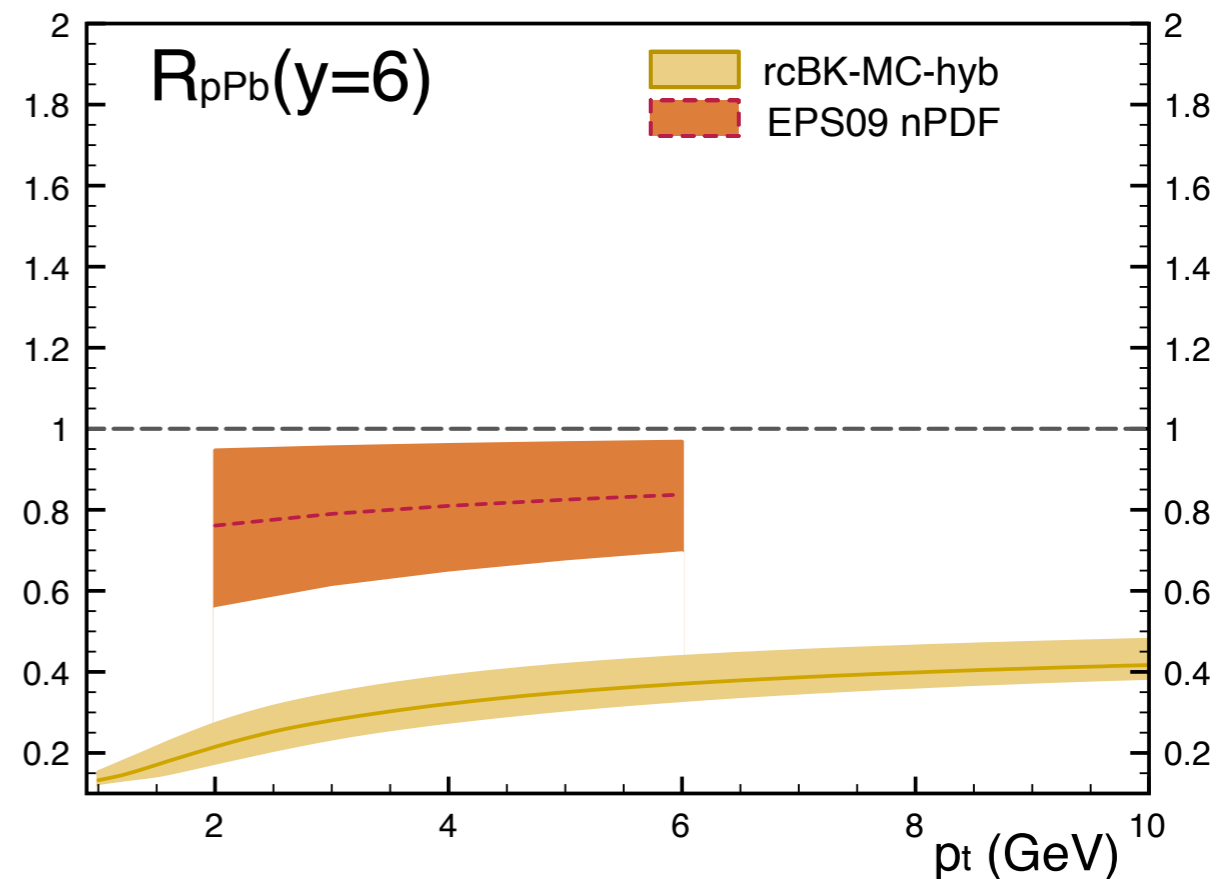
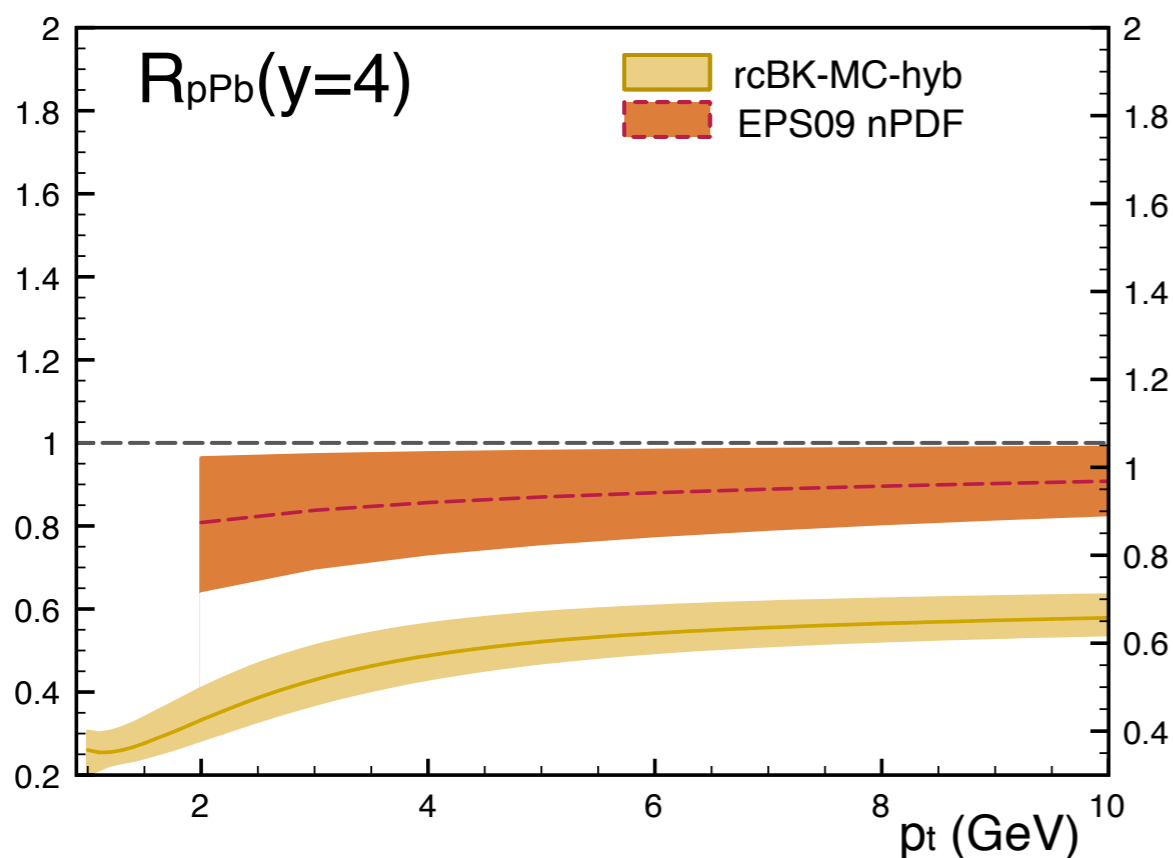
Moving forward: Testing the evolution



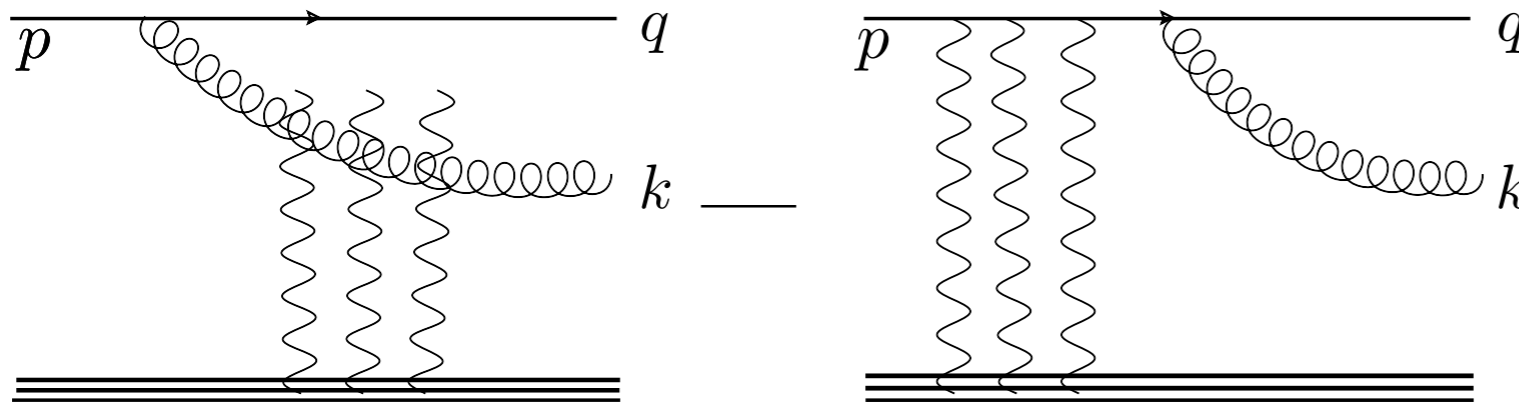
$(p_t, y_h \gg 0)$



Preliminary results. JLA-Dumitru-Fujii-Nara



CGC description: A quark (gluon) emits a gluon. The pair scatters independently off the target

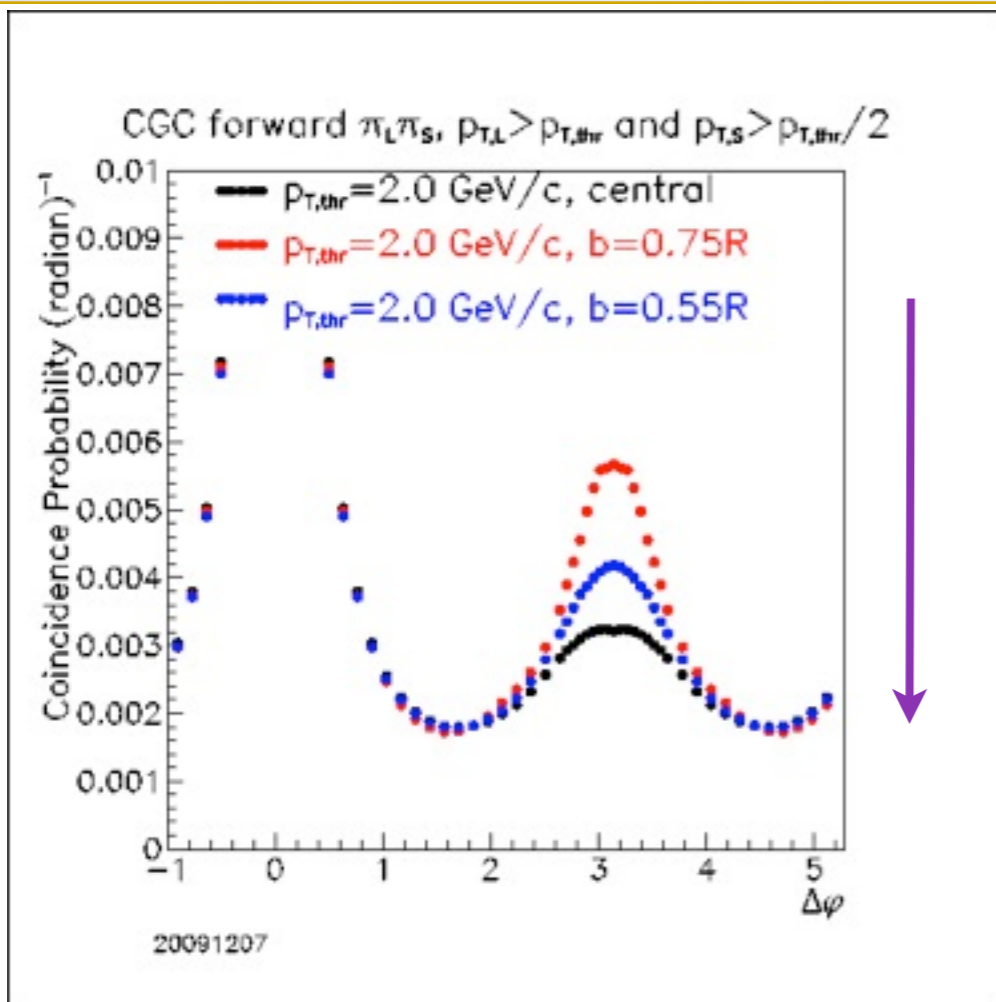


$$x_p = \frac{|k_1|e^{y_1} + |k_2|e^{y_2}}{\sqrt{s}}$$

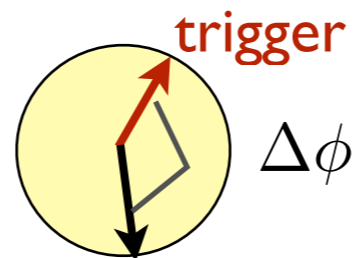
$$x_A = \frac{|k_1|e^{-y_1} + |k_2|e^{-y_2}}{\sqrt{s}}$$

At small- x , the transverse momentum transfer is controlled by the saturation scale

Angular decorrelation happens if $Q_s^{\text{Pb}}(\mathbf{x}_A) \sim (\mathbf{k}_1, \mathbf{k}_2)$



→ Coincidence probability



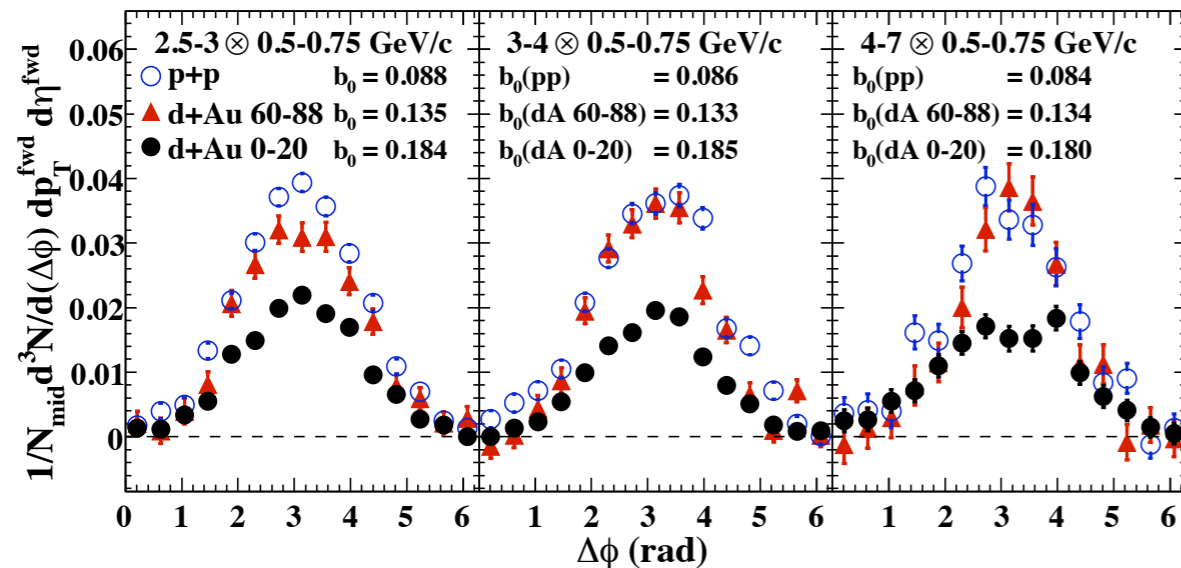
$$CP(\Delta\phi) = \frac{1}{N_{trig}} \frac{dN_{pair}}{d\Delta\phi}$$

Ergo, decorrelation should be stronger with

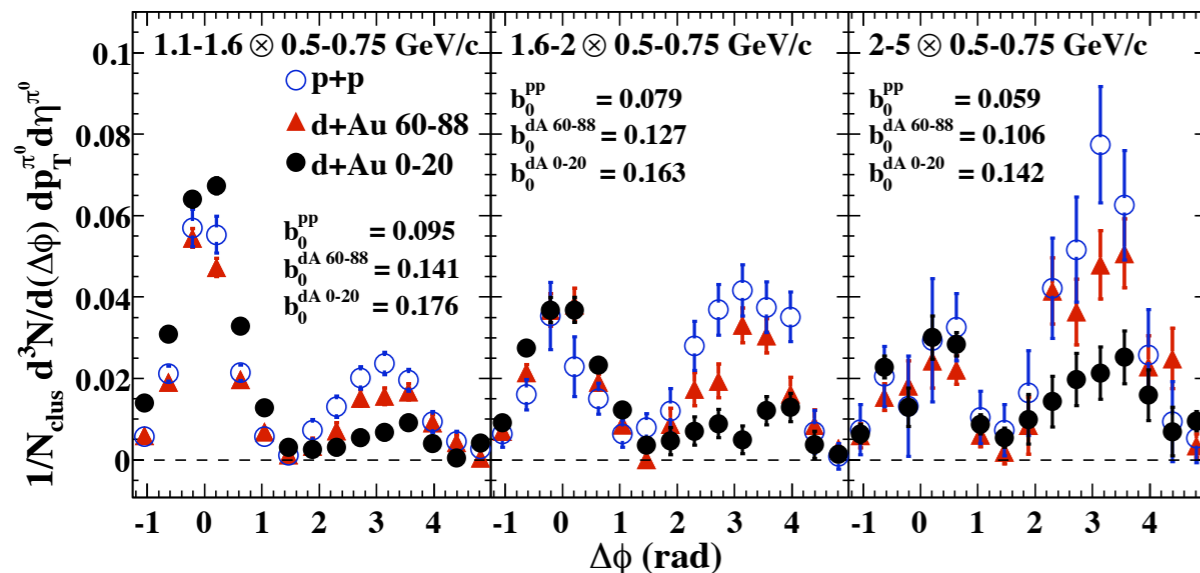
- Increasing rapidity of the pair
- Increasing collision centrality
- Decreasing hadron momentum

Forward di-hadron angular correlations in RHIC dAu data

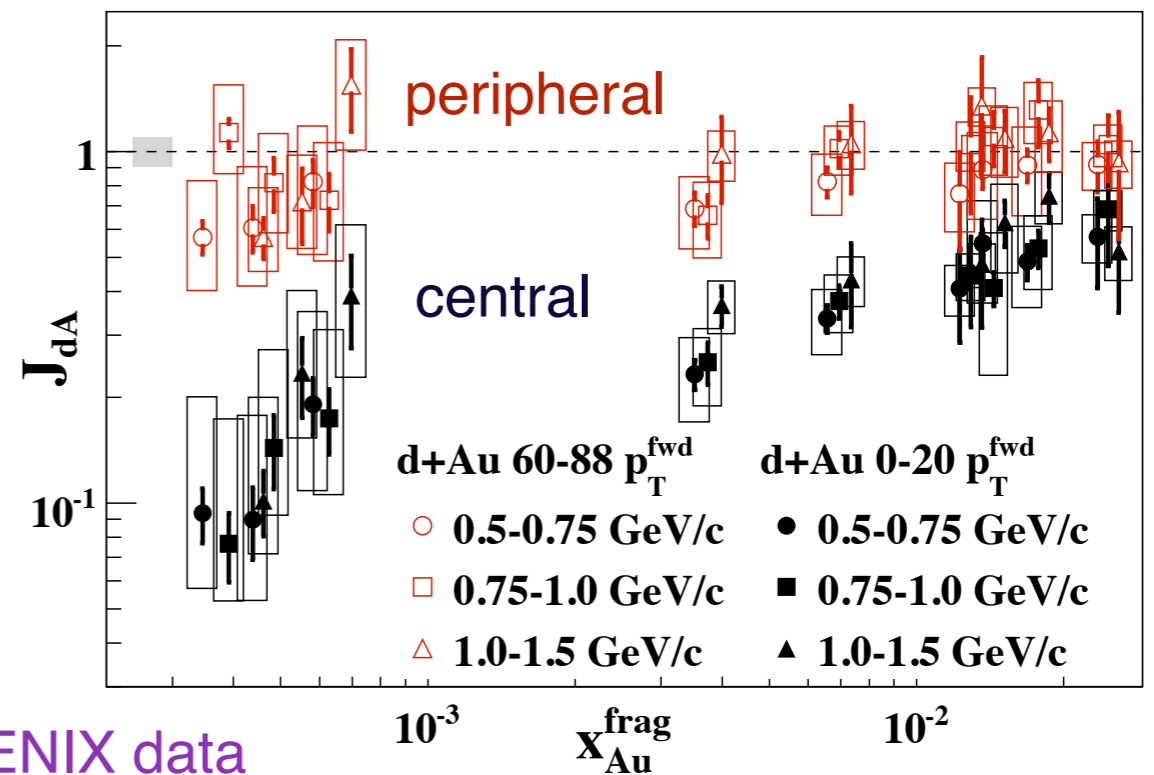
central-forward



forward-forward



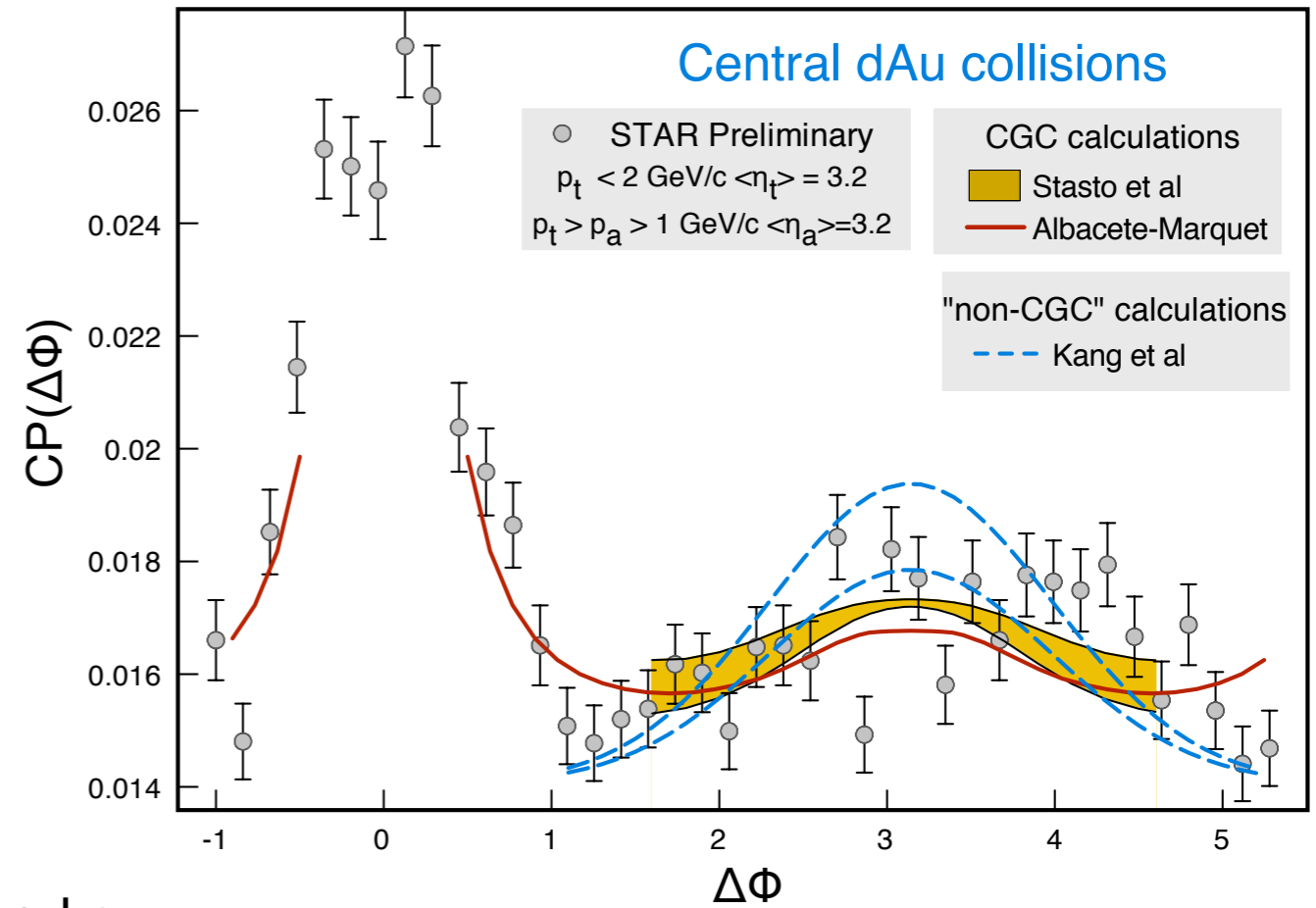
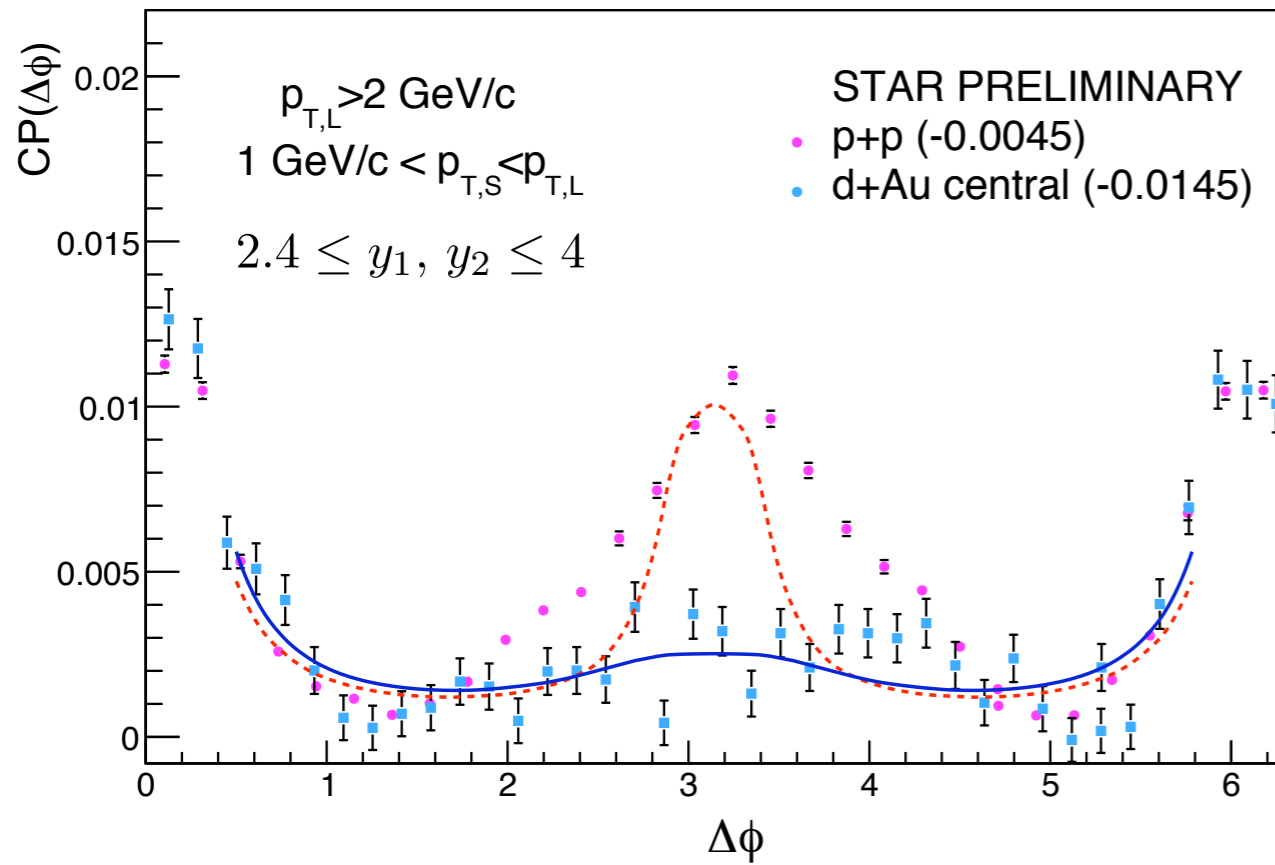
$$J_{dA} = I_{dA} \times R_{dA}^t = \frac{1}{\langle N_{\text{coll}} \rangle} \frac{\sigma_{dA}^{\text{pair}} / \sigma_{dA}}{\sigma_{pp}^{\text{pair}} / \sigma_{pp}}$$



Observed decorrelation IS stronger with

- Increasing rapidity of the pair
- Increasing collision centrality
- Decreasing hadron momentum

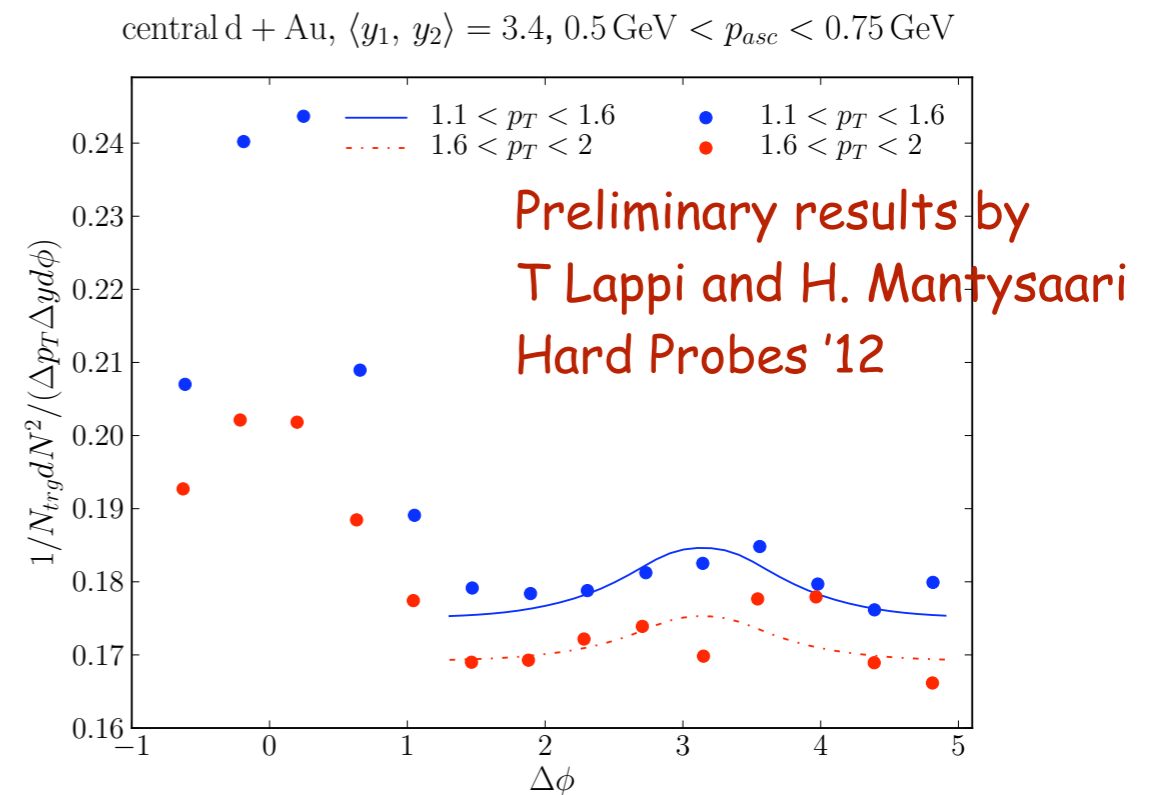
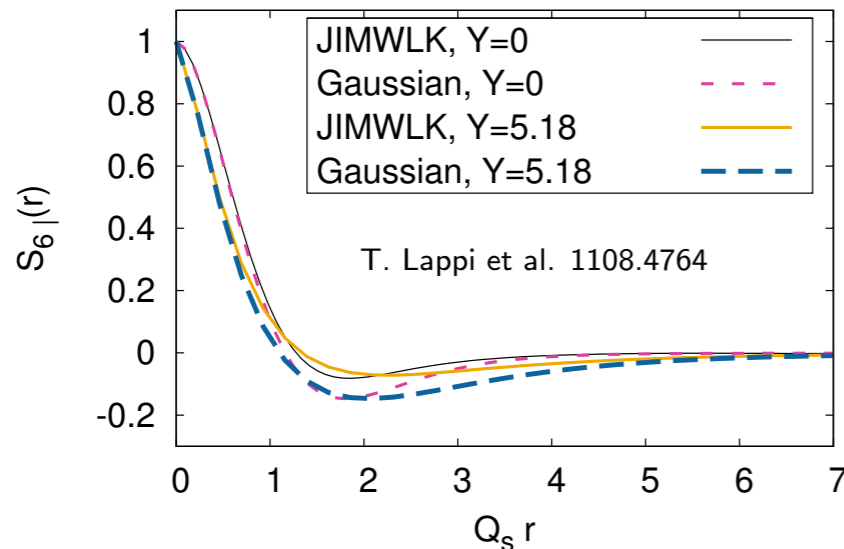
Forward di-hadron angular correlations in RHIC dAu data



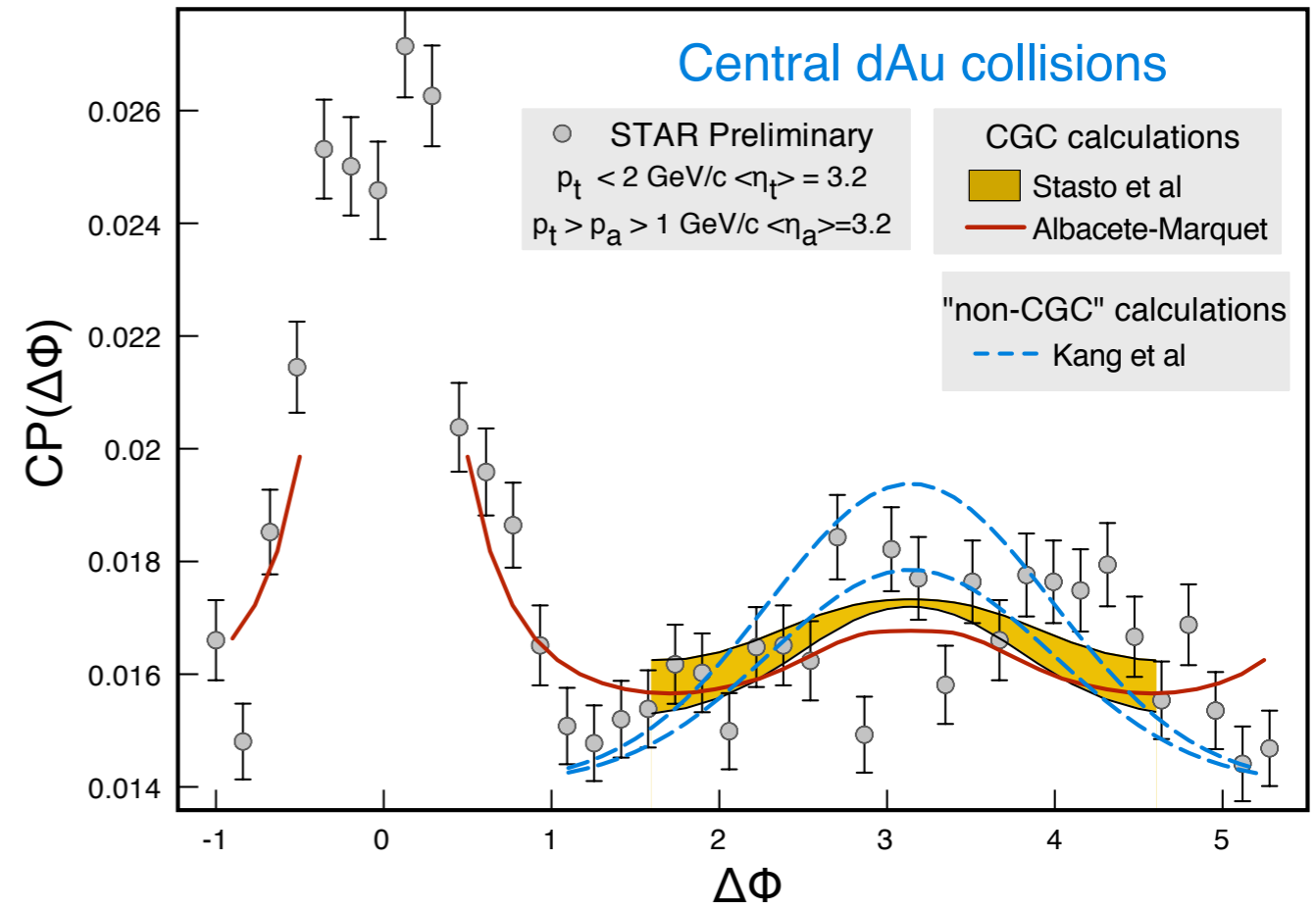
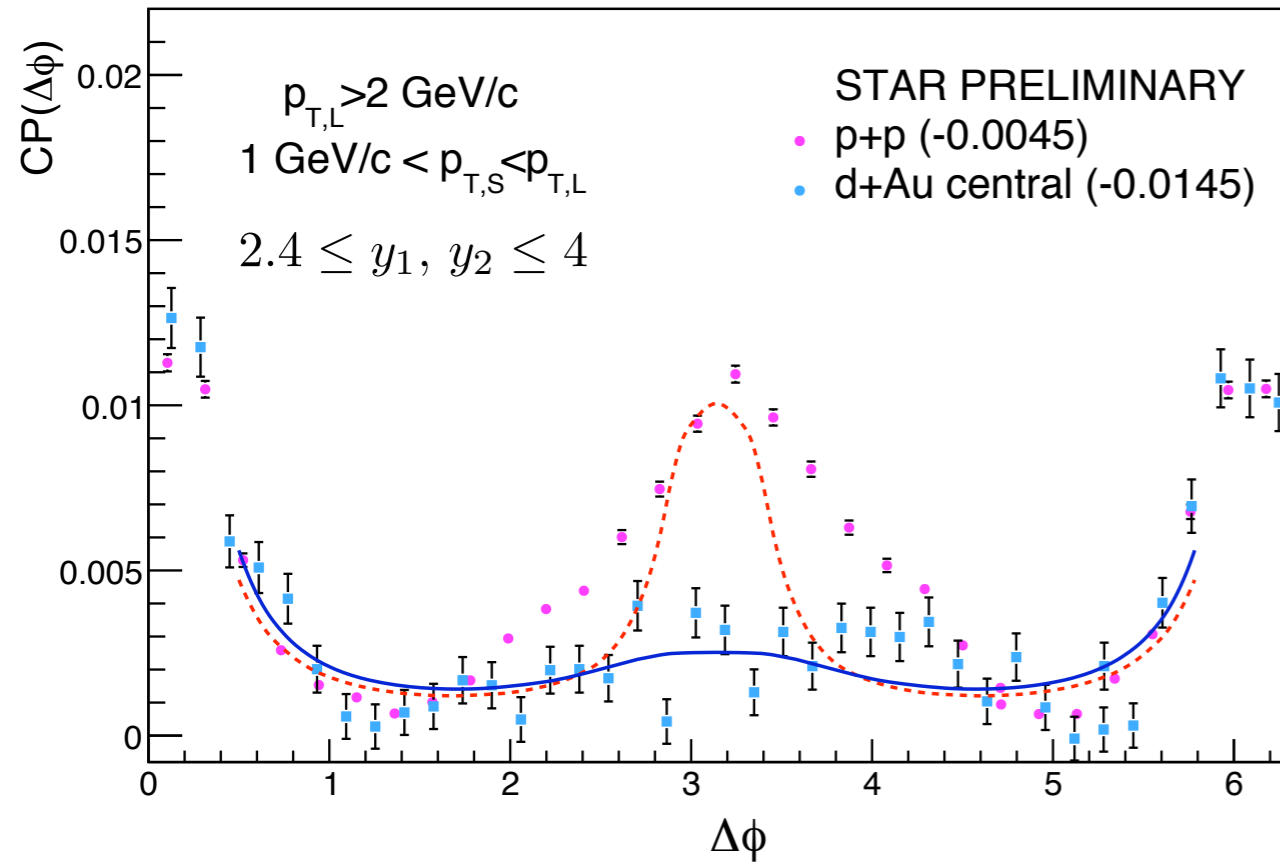
Uncertainties in current CGC phenomenological works:

- Need of a better description of n-point functions.

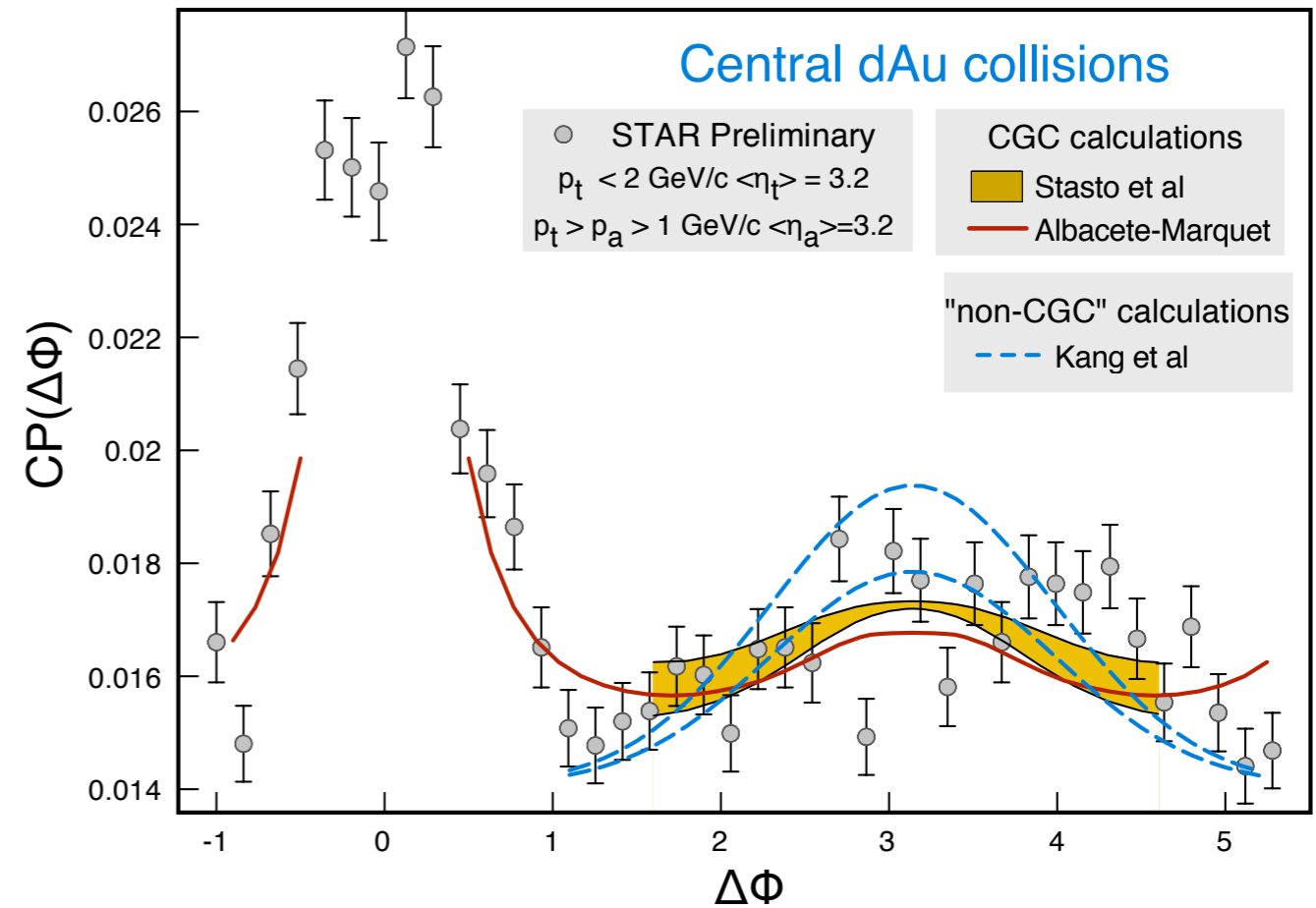
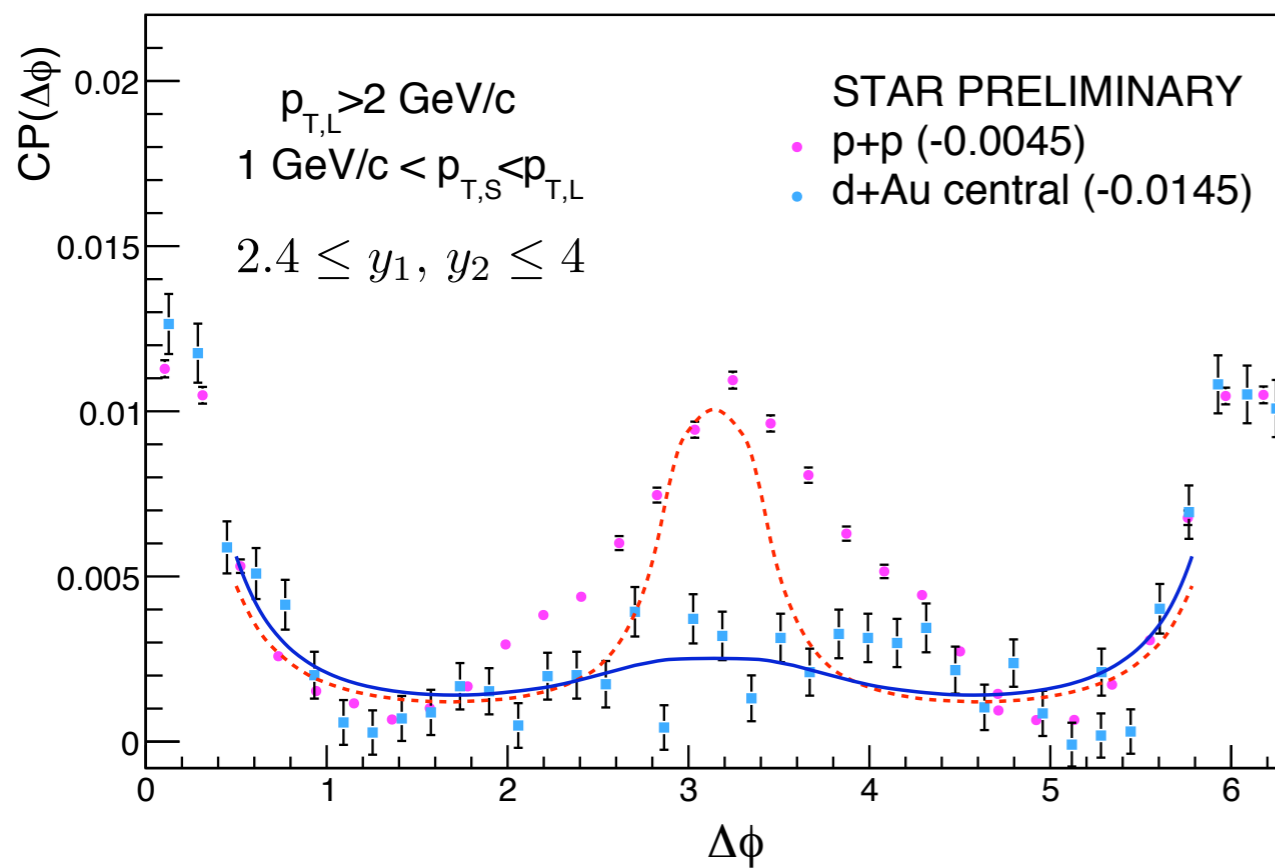
$$S^{(6)}(b, x, x', b') = Q(b, b', x', x)S(x, x') + \mathcal{O}\left(\frac{1}{N_c^2}\right)$$



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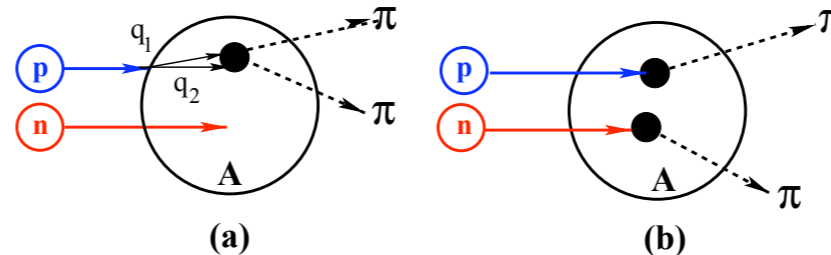


Uncertainties in current CGC phenomenological works:

- Need of a better description of n-point functions.
- Better determination of the pedestal: **K-factors in single inclusive production?**

Role of double parton scattering?

Strikman-Vogelsang



Strikman, Vogelsang, 1009.6123

- Alternative descriptions including **resummation of multiple scatterings, nuclear shadowing and cold nuclear matter energy loss** seem possible... [Kang et al]

Outlook

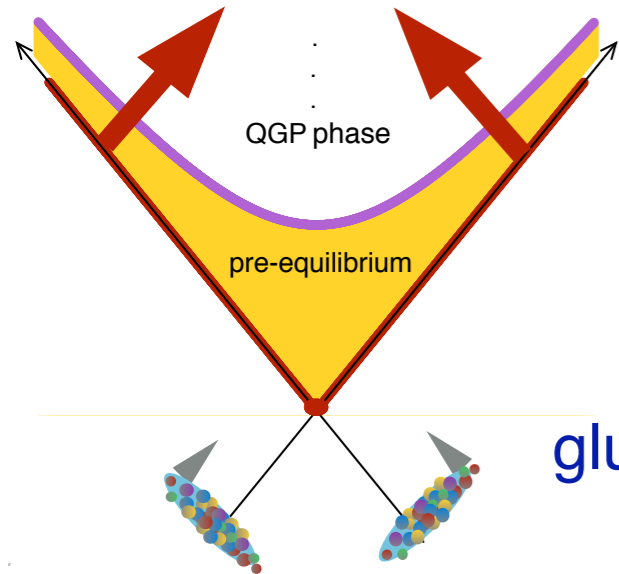
- ✓ Important steps have been taken in promoting GCG to an useful quantitative tool
 - Continuous progress on the theoretical side
 - Phenomenological effort to systematically describe data from different systems (e+p, e+A, p+p, d+Au, Aa+Au and Pb+Pb) in an unified framework
- ✓ Observed suppression phenomena in RHIC forward data provide the most compelling evidence for the relevance of CGC effects in presently available data
- ✓ However, RHIC data lies at the limit of applicability of the high-energy CGC formalism. Missing dynamical effects and higher order corrections may modify the interpretation of data
- ✓ More differential studies of data are needed to distinguish the CGC approach from others

Thanks!

Back up

Color Glass Condensate models

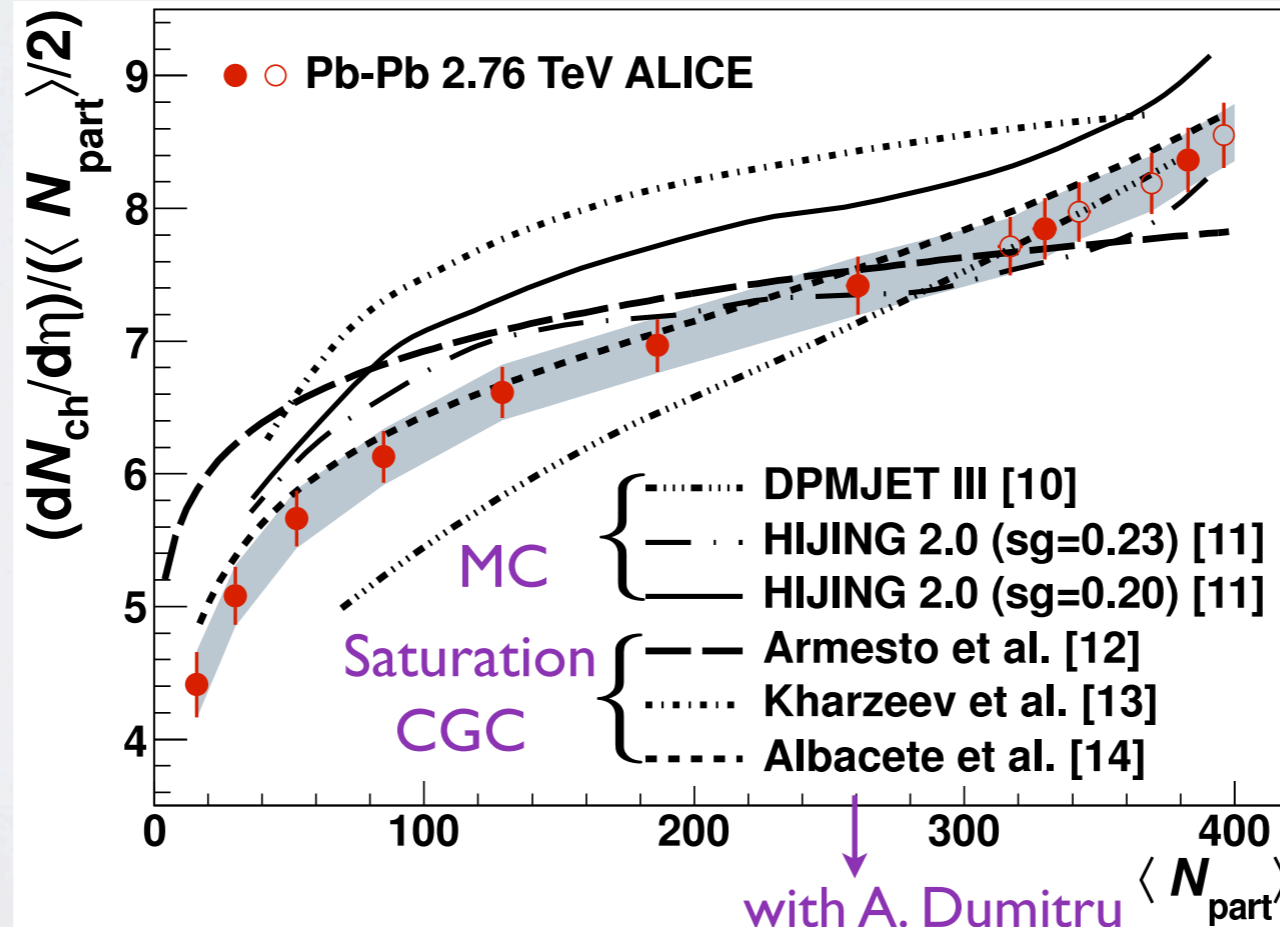
charged particles \sim # small-x gluons in the wave functions of the colliding nuclei



LO kt-factorization: $\left. \frac{dN^g}{d\eta d^2p_t} \right|_{\eta=0} \propto \frac{1}{p_t^2} \int d^2k_t \alpha_s \phi(\mathbf{x}_1, \mathbf{k}_t) \phi(\mathbf{x}_2, |\mathbf{p}_t - \mathbf{k}_t|)$

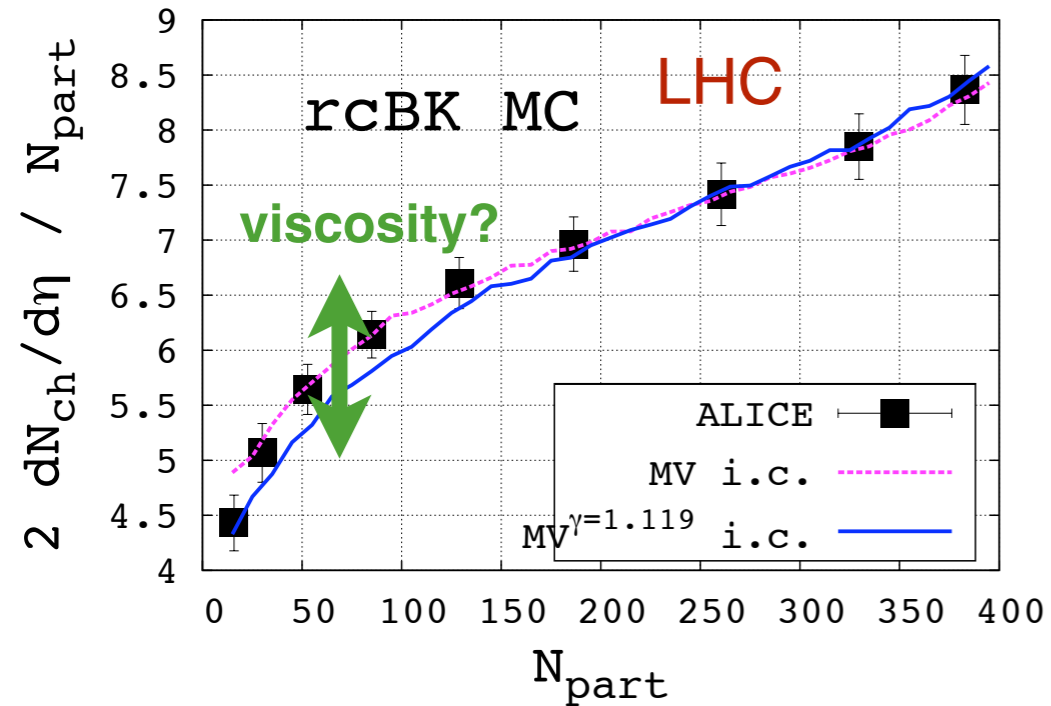
$$\lambda \approx 0.24 \div 0.3$$

gluon-hadron duality: $\left. \frac{dN^{ch}}{d\eta} \right|_{\eta=0} = \frac{2}{3} \mathbf{K} \left. \frac{dN^g}{d\eta} \right|_{\eta=0} \propto Q_s^2(\sqrt{s}, b) \sim \sqrt{s/s_0}^{-\lambda} N_{part}$



Miscellanea

- CGC gives a very good descriptions of bulk features of multiparticle production

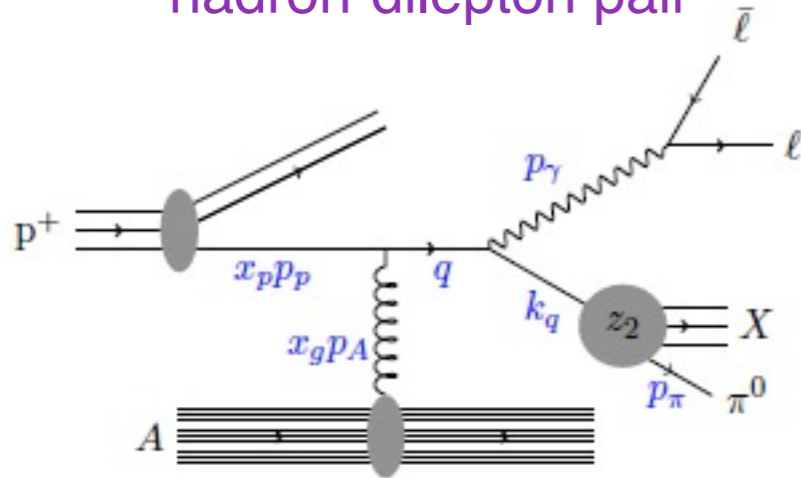


CGC: Non-linear and non-local

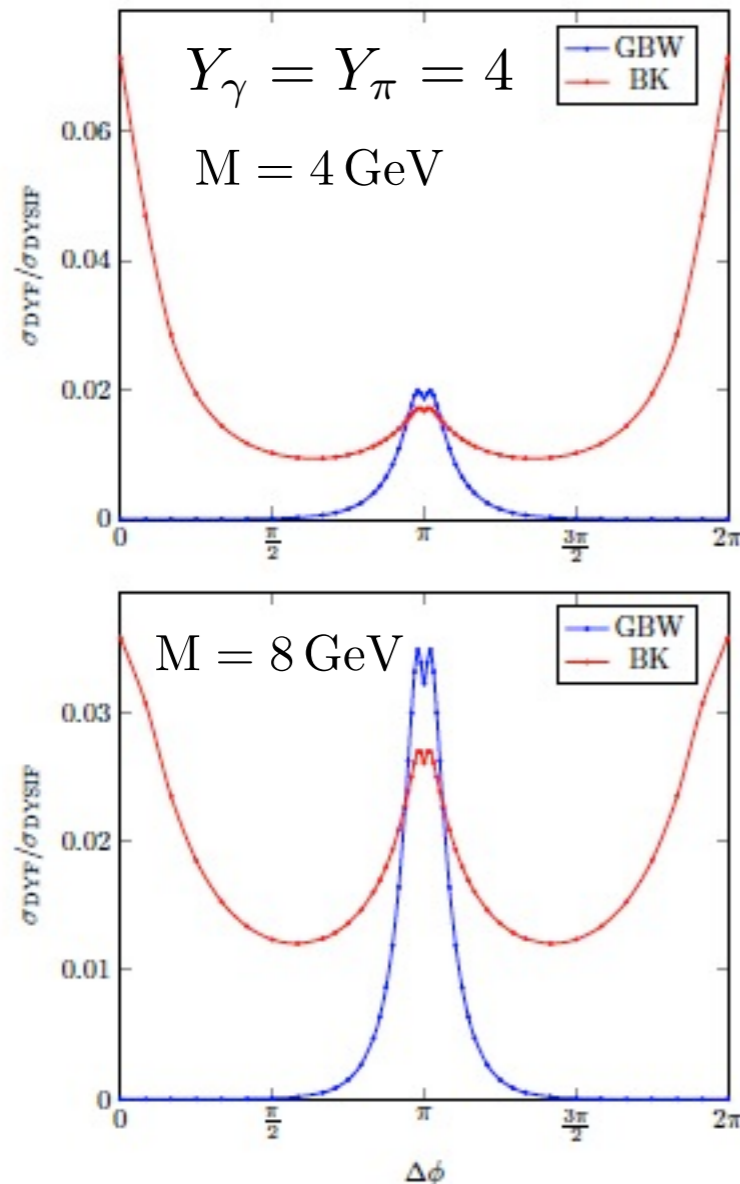
Knowledge of the “hard” part of nuclear UGD would further constrain the description of the initial state!

hadron-photon* correlations in pPb collisions at the LHC

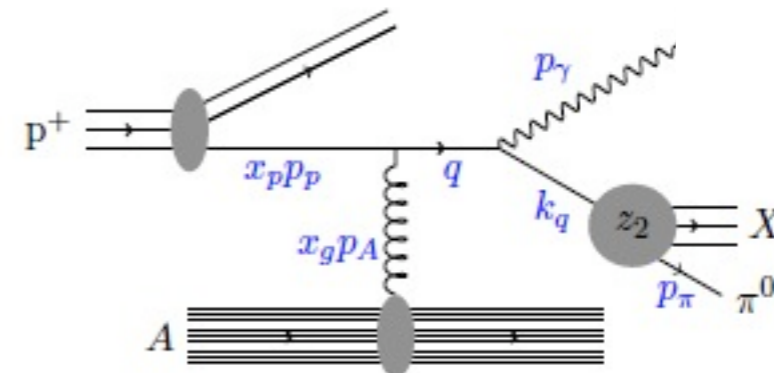
- hadron-dilepton pair



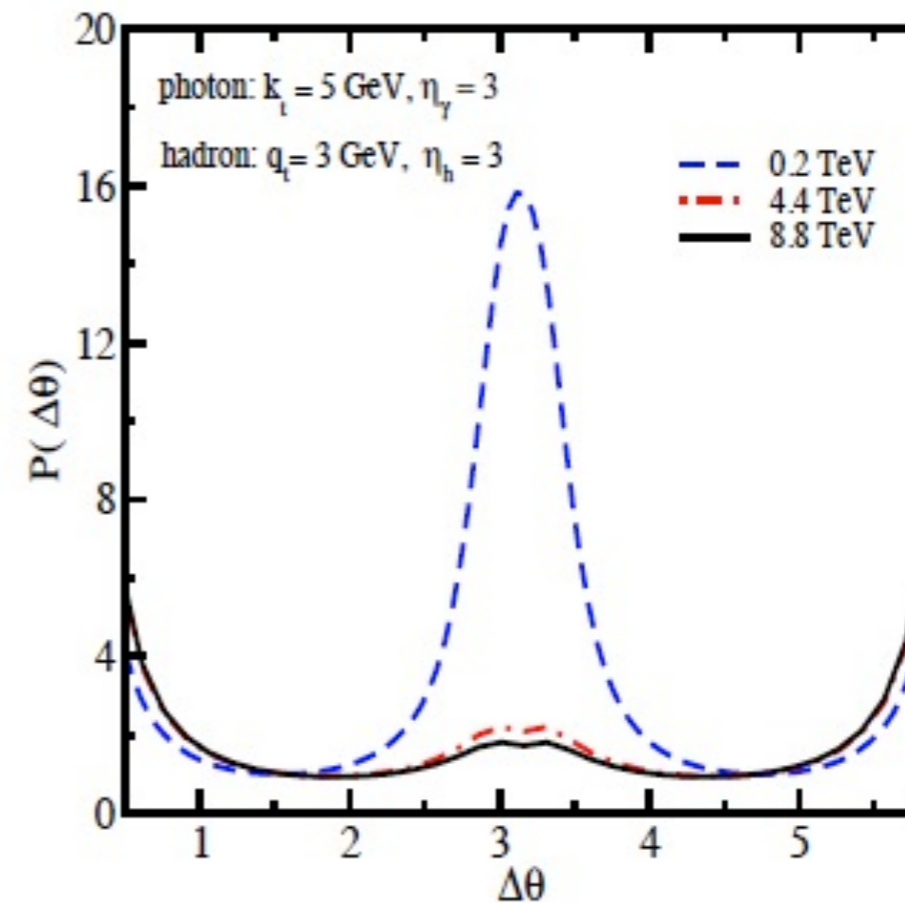
Stasto et al 1204.4861



- hadron-photon



Jalilian-Marian's talk



These processes are theoretically cleaner:
Only knowledge of 2-point needed!!